OPTOELECTRONIC WORKSHOPS

V

MODERN COHERENCE THEORY

May 18-19, 1988

sponsored jointly by

ARO-URI Center for Opto-Electronic Systems Research
The Institute of Optics, University of Rochester

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OPTOELECTRONIC WORKSHOP

ON

MODERN COHERENCE THEORY

Organizer: ARO-URI-University of Rochester and CECOM Center for Night Vision and Electro-Optics

- 1. INTRODUCTION
- 2. SUMMARY -- INCLUDING FOLLOW-UP
- 3. VIEWGRAPH PRESENTATIONS
 - A. Center for Opto-Electronic Systems Research Organizer -- Emil Wolf

Modern Coherence Theory Emil Wolf

B. Center for Night Vision and Electro-Optics Organizer -- Ward Trussell

Army Applications of Coherence Phenomena Ward Trussell

Detection of Laser Light and Holographic Filters Mark Norton

4. LIST OF ATTENDEES



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1. INTRODUCTION

This workshop on "Modern Coherence Theory" represents the fifth of a series of intensive academic/government interactions in the field of advanced electro-optics, as part of the Army sponsored University Research Initiative. By documenting the associated technology status and dialogue it is hoped that this baseline will serve all interested parties towards providing a solution to high priority Army requirements. Responsible for program and program execution are Dr. Nicholas George, University of Rochester (ARO-URI) and Dr. Rudy Buser, CCNVEO.

2. SUMMARY AND FOLLOW-UP ACTIONS

Dr. Rudy Buser of NVEOC made opening remarks in which he outlined the aim of the workshop and the relevance of coherence phenomena to some of the research activities that are in progress at the laboratory.

The workshop which followed consisted of two parts. In the first part Professor Wolf presented an account of the basic concepts of optical coherence theory. In particular he discussed the distinction between temporal and spatial coherence and concepts such as coherence time, coherence area, coherence volume, and the degeneracy parameter. He then introduced correlation functions that more fully characterize coherence properties of light. After this summary Professor Wolf presented a review of some of the more important recent developments. In particular he discussed coherent-mode representation of light of any state of coherence, coherence theory of laser modes, radiation from partially coherent sources, coherence properties of Lambertian sources and the effects of source coherence on the spectrum of the emitted light. Coherence effects in scattering of light from random media was also considered.

The second part was a morning session on the second day which consisted of an open discussion. It was started by Mark Norton of NVEOC who talked about practical applications of coherence. This was followed by a lively discussion regarding the possibility of making coherence filters. Suggestions were also made about future research on such devices and other applications to sensors and disscriminators, some of which mightautilize stratified media or holographic filters.

In addition to Professor Wolf the following scientists from the Unversity of Rochester took part in the workshop: Professor N. George, Dr. T. Stone, and Mr. B. Cairns. All of them participated in the discussion.

SUMMARY COMMENTS

MODERN COHERENCE THEORY - Dr. Emil Wolf May 18-19 1988

This workshop was of great interest to CNVEO personnel and was well attended. Coherence theory has direct application to Army programs in laser protection, detection of laser radiation, laser radar, vibration sensing, and communications. In the seminars on May 18, Dr. Wolf and Dr. Brian Cairns of Univ. of Rochester presented an excellent tutorial and overview of coherence research There was good interaction between CNVEO and Univ. of Rochester scientists in relating the theory to practical application. On Thursday, Mark Norton of CNVEO discussed the difficulties in detecting laser radiation remotely and optimizing a receiver for this purpose. There was further active discussion of the feasibility of 'coherence filters' for broadband laser protection. Dr. Wolf gave further insight in this topic and discussed a paper which will be published soon. He said that he planned to continue research in this area.

Most participants agreed that this workshop was valuable both for general understanding and for specific applications as outlined above.

C. Ward Trussell
C, Directed Energy Team
Laser Division

AGENDA

MODERN COHERENCE THEORY

Dr. Emil Wolf University of Rochester

Wednesday, May 18, 1988 - Main Conference Room, Bldg. 305

10:00 AM. - Introduction/Opening Remarks - CNVEO

10:05 - Modern Coherence Theory - Dr. Wolf Univ. of Rochester

Noon - Lunch

1:30 - 4:00 - Coherence Theory, continued

Dr. Wolf,

Univ. of Rochester

Thursday, May 19, 1988 - The Arena, Bldg. 309

9:00 - Practical Applications of coherence - Mark Norton CNVEO

9:15 - Open Discussion -

- 1. Can coherence filters be made?
- 2. What theoretical research needs to be done?
- 3. What experiments have been done?
- 4. What experiments should be done?
- 5. What are the coherence properties of photorefractive filters.
- 6. Other applications of this research.

11:00 - Recommendations for continued research/study

Noon - End

CENTER FOR OPTO-ELECTRONIC SYSTEMS RESEARCH MODERN COHERENCE THEORY

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1.	REVIEW OF ELEMENTARY CLASSICAL COHERENCE THEORY
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For fuller reviews of elementary classical coherence theory, see

- M. Born and E. Wolf, <u>Principles of Optics</u> (Pergamon Press, Oxford and New York, 6th ed., 1980), chapt. X.
- E. Wolf, "Basic concepts of optical coherence theory" in Proc.Symp. on Optical Masers, ed. J. Fox, (Brooklyn Polytechnic Press and J. Wiley, 1963), pp. 29-42.
- L. Mandel and E. Wolf, "Coherence properties of optical fields", Rev. Mod. Phys. 37, pp. 231-287 (1965).
- J. Perina, Coherence of Light (Reide., Boston, second ed., 1985).
- J. W. Goodman, Statistical Optics (Wiley, New York, 1985).

UA) = aH) en[qH-Et]

(Quasi-monochromete Lyle)

At P :

(4) = a,4) en [9,4) - = 4]

 $U_2(t) = q_2(t) \cos [P_2(t) - \omega t]$

At P:

 $I\omega = [U, \omega + Q, \omega]^2$

a, cos [14-2+] + 4, ca [1/2-2+]

+9,2 cos[4,12-226] +9,2 cos(12-12) (4)

Suppose
$$a_1(t) = a_2(t) = c_m cd(t=a)$$
 (s)
 $a_1(t) = a_2(t) = c_m cd(t=a)$ (s)

$$\langle I(+) \rangle = \frac{1}{2}a^2 + \frac{1}{2}a^2 + 0 + a^2 \langle \omega_3(q_1 - q_2) \rangle$$

$$= a^2 \left[1 + \langle \omega_3(q_1 - q_2) \rangle \right]$$

$$= a^2 \left[1 + \langle \omega_3(q_1 - q_2) \rangle \right]$$
Therefore term

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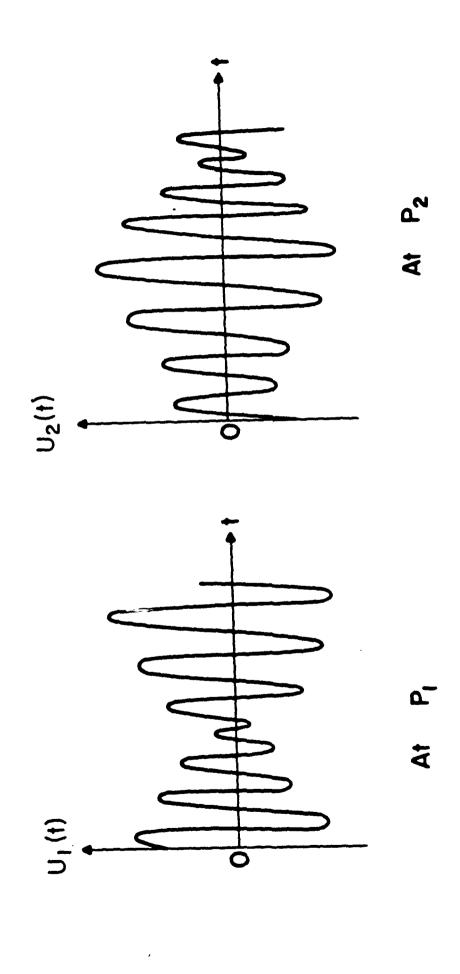
0 < (I(+)> < 2a2

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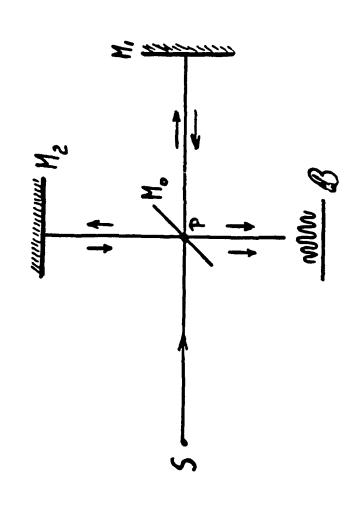
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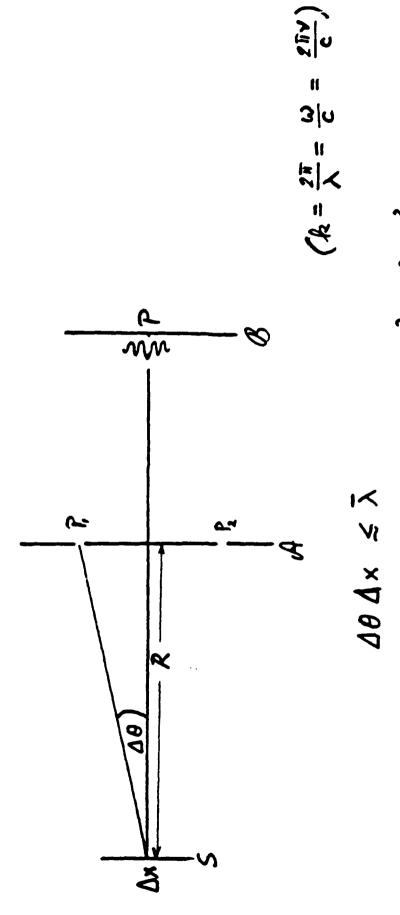
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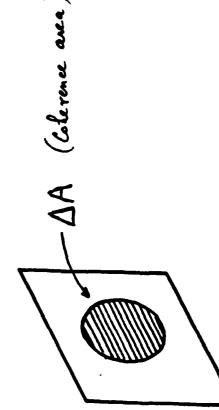
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Spahal coberence and coberence area



 $\Delta A \sim (R\Delta\theta)^2 \sim R^2 (\frac{\lambda}{\Delta^2})^2 = \frac{c^2}{5^2} \frac{R^2}{S} \left[S = (\Delta x)^2 \right]$

Chumer area:



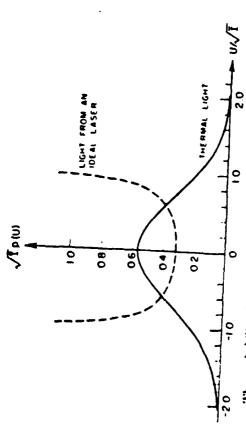
S

For blackbody radiation:

$$E_y = \frac{2y^2}{C^3} \frac{1}{\phi^{4y/4T}-1}$$
 (

DIFFERENCES AND TYPICAL VALUES

	Thermal Source	Laser
Emission	spontaneous (for T≤50,000°K)	stimulated
Minimum bandwidth (Δν)	10 ⁹ Hz	1 Hz
Coherence time (∆t)	10 ⁻⁹ sec	1 sec
Coherence length (Δ)	1 m	10 ⁹ m
Maximum degeneracy (δ)	10 ⁻³	10 ³ - 10 ¹⁵
Probabilities: p(U)	~ e ^{-U²/σ²}	$\sim \frac{1}{\sqrt{\overline{1} \cdot U^2}}$
p(1)	~ e ^{-I / Ī}	~ S (1- T)



The probability densities relating to thermal light and to light from an ideal Congress, edited by N. Bloembergen and P. Grivet, New York: Columbia University Press; Paris: Dunad, p. 101.)

$$U(t) = \int_{a(\omega)} e^{-i\omega t} d\omega \qquad (1)$$

Red if:
$$v(t) = \int v(\omega)$$

Analyte signal:
$$V(t) = \int \sigma(\omega) e^{-i\omega t} d\omega$$
 (3)

 $\xi_1 = \tau_1/c$

 $\xi_2 = \tau_2/c$

$$V(P,t) = K_1 V(P_1, t-t_1) + K_2 V(P_2, t-t_2)$$

$$I(P) = \langle V(P_1, t) V^*(P_1, t) \rangle$$

$$= \langle V(P_1, t) V^*(P_1, t) \rangle$$

$$= \langle V(P_1, t) V^*(P_1, t) \rangle$$
interference term

Mutual Coherence function:

$$\int_{12} (\tau) = \langle V(P_1, t+\tau) V^*(P_2, t) \rangle$$
 (2)

$$\nabla_{j}^{2} \Gamma_{l}(\tau) = \frac{1}{c^{2}} \frac{\partial^{2} \Gamma_{l}(\tau)}{\partial \tau^{2}}, \quad (j=1,2)$$
 (3)

$$J_{12}(x) = \frac{J_{12}(x)}{J_{17}(0)} \frac{J_{12}(x)}{J_{12}(0)}$$
 (1)

$$0 \le |\gamma_2(\tau)| \le 1$$
incolumna

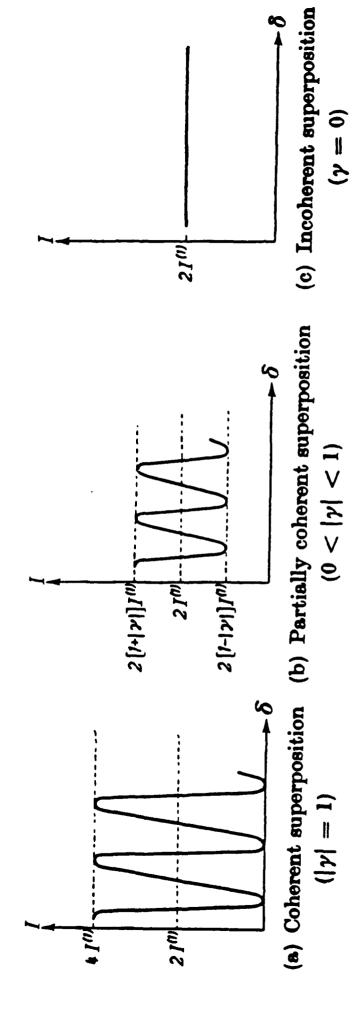
Indeference law:
$$(\frac{\Delta \nu}{\omega} \ll 1, |\delta| \ll \frac{\omega}{\Delta \omega}, I^{(1)} = I^{(1)})$$

$$I(P) = 2I''(P)\{1+13_{12}(r)|c_{23}[c_{23}c_{23}-5]\}$$
 (2)

$$\alpha_{12}(r) = ang \, \partial_{12}(r) + \overline{\omega} \, r$$
, $S = \overline{\omega} \, r$, $r = \frac{r_2 - r_1}{c}$ (3)

Wisibility of finges:

$$\mathcal{Y}(p) = \frac{I_{max} - I_{min}}{I_{max} + I_{min}} = |\eta_2(r)| \quad (4)$$



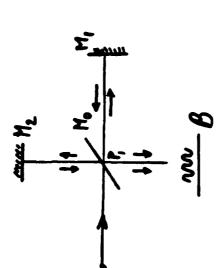
Intensity distribution in the interference pattern produced by two quasimonochromatic beams of equal intensity $I^{(1)}$ and with degree of coherence $|\gamma|$.

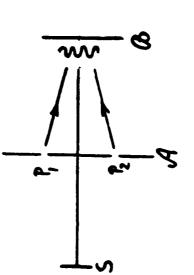
$$J_{12}(z) = \frac{J_{12}(r)}{\sqrt{J_{10}(0)}}$$

$$0 \le \left| \gamma_{12}(z_1) \right| \le 1$$

incoherence

complete colerence



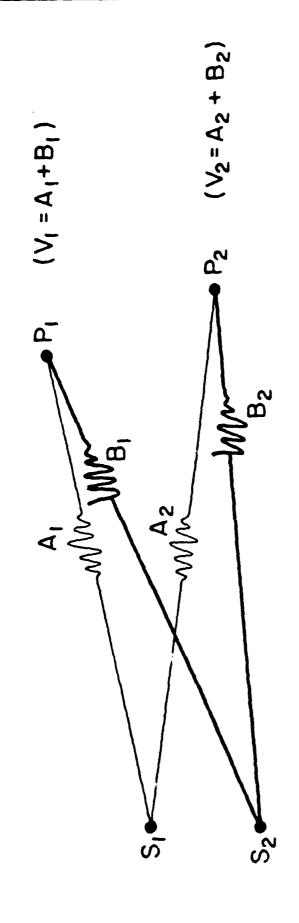


Temporal colerence: The (T)

Spaked columna: 8,2(0)

Visibility of finges: 181 Position of minima and making: ang 8

GENERATION OF SPATIAL COHERENCE FROM UNCORRELATED SOURCE



$$=0, (i,i=1,2)$$

(12)

(13)

(14)

$$A_2 \approx A_1$$
 $B_2 \approx B_1$

$$At P_i: V_i=A_i+B_i$$

Generator of stated coherence from an incoherent source

The ran Cithet-terms has

6 G

(2:15) $\nabla_{j}^{2} \prod_{l} (\varepsilon) = \frac{l}{c^{2}} \frac{\partial^{2} \prod_{l \neq l} (\varepsilon)}{\partial z^{2}}$

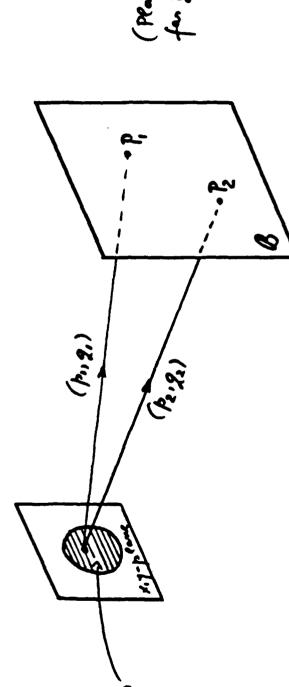
Tropagation of coherence:

Goundary Conditions:

[(a,,a,,r) = 1/02-0,) 5/02-0,)e P(P, P, 0) = / 1/0, e. 1/2.

Solution:

VAN CITTERT - ZERWIKE THEOREM 0 F FAR- ZONE FORM

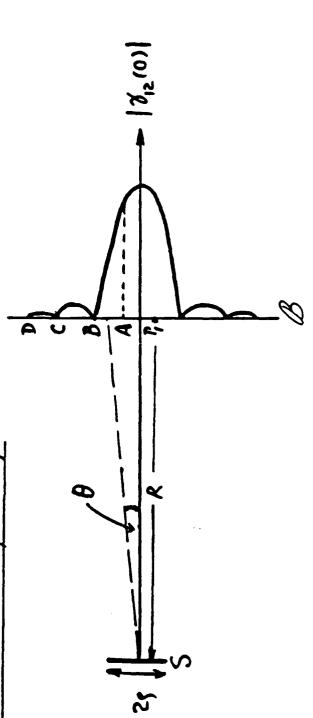


(Peme B in the for 3 source)

 $\mathcal{J}_{12}(0) = \frac{1}{N} \iint j (x, y) e^{-i \vec{k} [(p_1 - p_2)x + (g_1 - g_2)y]} dx dy$ (1)

 $N = \iint_S dxdy \qquad (2)$

Uniform avaules from ce of marties p.



$$\frac{Q_{n}(B)}{N_{12}(0)} = \frac{2J(n)}{2J(n)}$$

(AR >1)

Sin
$$\theta \sim 0.61\lambda/g$$

 $\sin \theta \sim 1.11\lambda/g$

%

(degree of polarization) (4a) (94) Gardal polerization - Coherency matrices $1 - \frac{4/\xi}{(7,\xi)^2}$ $0 \le |\mu_{xy}| \le 1$ Max /my/ = P **€**(±)

Mutual coherence tune from

$$\Gamma_{(\underline{x}_1,\underline{x}_2,\tau)} = \langle V_{(\underline{x}_1,t+\tau)} \rangle^{t}_{(\underline{x}_2,t)} \rangle$$

Columency fensors

$$\xi_{j_{K}}(\underline{x}_{i},\underline{x}_{i},\tau) = \langle \xi_{j}(\underline{x}_{i},+\tau\tau) \xi_{K}^{*}(\underline{x}_{s},\tau) \rangle$$

$$\mathcal{H}_{jk}(\underline{x},\underline{x},\tau) = \langle H_j(\underline{x},t+\tau) H_k^{\star}(\underline{x},t) \rangle$$

$$\mathcal{M}_{jk}(\underline{x},\underline{x},\tau) = \langle E_j(\underline{x},t+\tau) H_k^{\star}(\underline{x},t) \rangle$$

$$V_{jk}(k_1,k_2,\tau) = \langle H_j(k_1,t+\tau) E_k^*(k_2,t) \rangle$$

$$(j, \kappa = \kappa, y, \epsilon)$$

$$\sum_{j=1}^{2} \sum_{j=1}^{2} \sum_{j$$

$$a_{x}^{2} = \frac{\partial}{\partial x^{R}} (R = 1, 2, 3)$$

= < V(E, t,) V" (E, t,) V" (x, t,) V (x, t,) V (x, t, t, t,) Mutual colerence function (2nd order): \(\(\text{\else}_{1, \text{\else}_{2, \text{\else}}} \) = \(\(\text{\else}_{1, \text{\else}_{2, \text{\else}}} \) = \(\(\text{\else}_{1, \text{\else}_{2, \text{\else}}} \) = \(\(\text{\else}_{1, \text{\else}_{2, \text{\else}}} \) Charenes function of order (m,n) - scales felt Hylen-order columne functions (tenson) M(m,m) (xs, x2, ... xm+n) t, t2, ... tm+n)

Cheenee denton of order (m,n) - P.m. feld

= $\langle \vec{E}_{i}^{*}(\underline{v}_{i},t_{i}) \vec{E}_{i}^{*}(\underline{x}_{2},t_{2}) \dots \vec{E}_{i}^{*}(\underline{x}_{n},t_{n}) \vec{E}_{i} (\underline{x}_{n+1},t_{n+1}) \dots$ er (m.m.) 4 dz ... - Juson

k fr (m,m) fr, je,... jm+m,

+

22

... E. (xata, tata)

(1/5) = < NUT (+=) 1/4 (5,4)> 0) MUTUAL COHERENCE FUNCTION:

CROSS-SPECTRAL DENSITY:

$$\mathcal{N}(\underline{x}_i,\underline{x}_e,\omega) = \frac{1}{2\pi} \int f'(\underline{x}_i,\underline{x}_e,\tau) e^{i\omega \tau} d\tau \qquad \alpha$$

$$V(\underline{x},\omega) = \frac{1}{2\pi} / V(\underline{x},t) e^{i\omega t} dt \qquad (3)$$

$$\langle v(\underline{r},\omega)\eta^*(\underline{r},\omega')\rangle = W(\underline{r},\underline{r},\omega)\delta(\omega_{-\omega})$$

COMPLEX DEGRÉE OF SPECTRAL COHELENCE:

$$\mu(\underline{r},\underline{r},\omega) = \frac{W(\underline{r},\underline{r},\omega)}{|W(\underline{r},\underline{r},\omega)|} / W(\underline{r},\underline{r},\omega)$$

MM

F. F. are identical narrow-dand filters

The) is the complex amplifude housewithen turken of each filter

$$V(P_{i}, \omega) \longrightarrow T(\omega) V(P_{i}, \omega) \qquad (\dot{I} = i, 1)$$

E

$$\langle T(\omega) v(R,\omega) T^*(\omega) v^*(R,\omega) \rangle = W^{(+)}(R,R,\omega) \delta(\omega-\omega')$$
 (9)

$$W^{\bullet}(\mathcal{R}, \mathcal{R}, \omega) = (T_{(\omega)})^2 W(\mathcal{P}, \mathcal{R}, \omega) \tag{n}$$

$$\Gamma^{(4)}(P_{\mu}P_{\mu}z) = \int |T(\omega)|^2 W(P_{\mu}P_{\mu}\omega) e^{-i\omega \tau} d\omega$$
 (11)

F. WOLF OLL LAH. 8.250 (1983): P. DESANTIS, F. GORI, G. GUATTARI, C. PALHA, J.H. NEBSTEK,

25

4 dos is softwarty small (see fifue), Eq.(11) gras

JW (P, P, w)

=

(13)

O(=) = filt fuctor

$$|| h_{ex} || (9/c)|| = || \theta(0)|| = 4$$

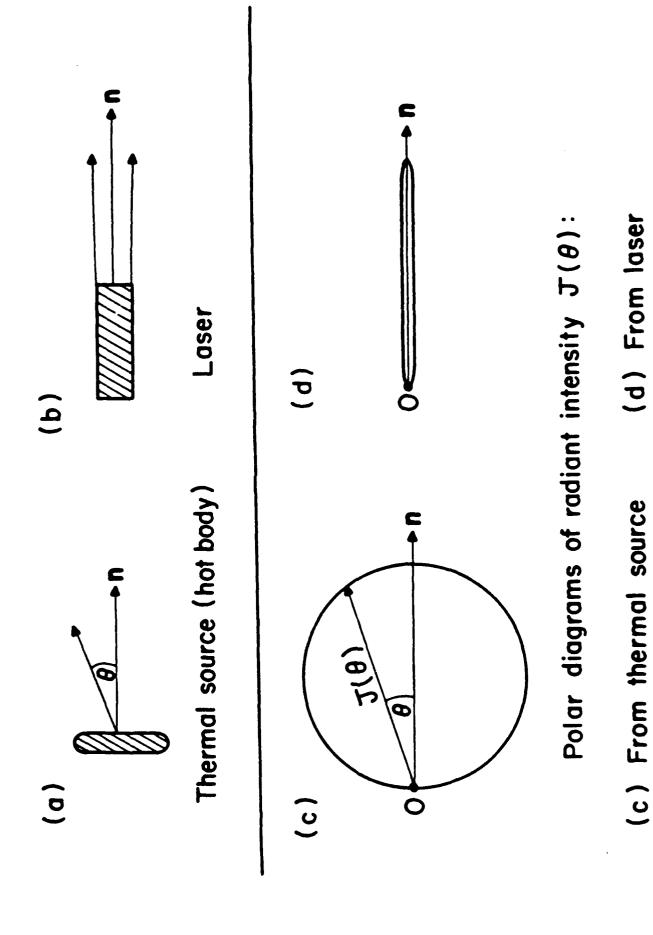
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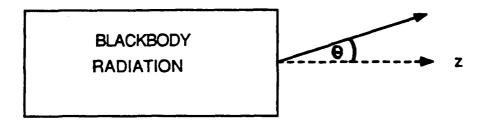
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: pe is a measurable quantity. - ANTHUMPHOR (%) $(\omega_{\nu})_{\nu} << (\omega_{\nu})_{\nu}$ [(18)] Imax (E) + Imin (E) (Lana) (L. 2, 2) | = | (2, 2, 1) | (1, 2, 12) Imax (c) - Imam(c) (20) 1(4)(4,2,2) = /4(1,2,00) B(E) 360) T(+, 2,0) = /4 (2, 2, 00) Kribitify O(T) -- Affle--V(z) **(**∇0)′

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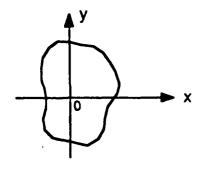


RADIATION FROM THERMAL SOURCES

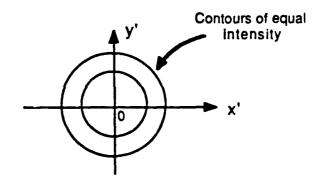


LAMBERT'S LAW

 $J(\theta) = J(0) \cos \theta$



SHAPE OF EFFECTIVE SOURCE

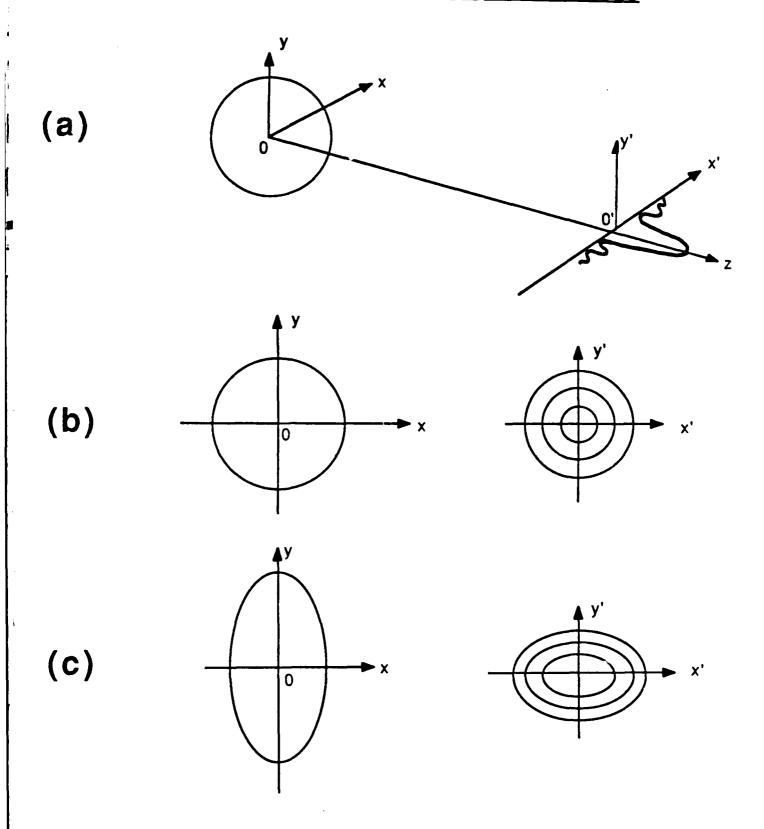


FAR-FIELD PATTERN

FAR-FIELD <u>INTENSITY PATTERN</u> IS <u>ROTATIONALLY</u>

<u>SYMMETRIC</u> ABOUT THE NORMAL TO THE SOURCE PLANE,

<u>IRRESPECTIVE OF SHAPE OF SOURCE</u>



RECIPROCITY

RADIANT INTENSITY

THERMAL SOURCES
(SPATIALLY INCOHERENT)

LASER SOURCES
(SPATIALLY COHERENT)

Broad angular distribution (Lambert's Law)

Narrow angular distribution (exponential-Gaussian)

Independent of shape of source
(always rotationally
symmetric)

Strongly dependent on shape of source
(in general not rotationally symmetric)

PROPAGATION OF THE CROSS-SPECTRAL DENSITY

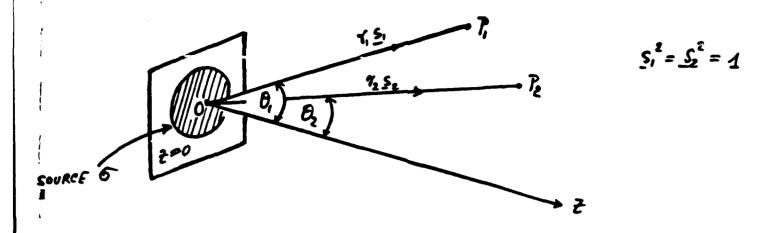
$$\nabla_{i}^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) + \lambda^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) = 0$$

$$\nabla_{i}^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) + \lambda^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) = 0$$

$$\nabla_{i}^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) + \lambda^{2} W(\underline{x}_{i}, \underline{x}_{i}, \omega) = 0$$
(1)

$$(2i-i)$$
 , $\frac{1}{2e} + \frac{3e}{2e} + \frac{1}{2e} + \frac{1}{2e} = \frac{1}{2}$

FAR-ZONE BEHAVIOR*



$$W^{(\infty)}(x,s_1,x_2,s_2,\omega) = (2\pi\hbar)^2 W^{(0)}(ks_{11},-ks_{21},\omega) \frac{e^{ik(x_1-x_2)}}{x_1x_2} \cos\theta,\cos\theta_2 \quad (4)$$

$$(kx_1-x_2) \cos\theta_1 \cos\theta_2 \quad (4)$$

$$\tilde{W}^{(e)}(\underline{f}_{1},\underline{f}_{2},\omega) = \frac{1}{(2\bar{n})^{4}} \int W^{(e)}(\underline{f}_{1},\underline{\gamma}_{2}',\omega) e^{-i(\underline{f}_{1},\underline{\gamma}_{1}'+\underline{f}_{2},\underline{\gamma}_{2}')} d_{\underline{\tau}_{1}'}^{2} d_{\underline{\tau}_{2}'}^{2}$$
(5)

$$f_1 = h s_{11}$$
, $f_2 = -h s_{21}$ (6)

LOW STATIAL-FREQUENCY COMPONENTS

* E. W. MARCHAND and E. WOLF, JOH. Soc. Amer., 62, 379 (1972)

OPTICAL INTENSITY IN THE FAR FIELD:

$$I^{(a)}(r_{5}) = \frac{J_{(5)}}{r^{2}}$$
 (8)

PADIANT INTENSITY (in director & making augh B with mound to some plane):

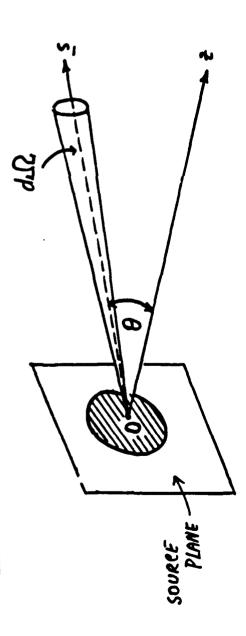
$$J(s) = (2\pi k)^2 \sqrt{^{(0)}} (k_{S_L}, -k_{S_L}) \cos^2 \theta$$
 (9)

DEGREE OF SPECTRAL COHERENCE OF FAR FIELD:

$$\mu''(q_{5,72}, z_{5,2}) = \frac{\widetilde{W}^{(0)}(h_{5,11}, -h_{5,21})}{\sqrt{\widetilde{W}^{(0)}(h_{5,11}, -h_{5,21})}} e^{ih(x_1 - x_1)} e^{ih(x_1 - x_2)}$$
(10)

(Dependence on frequency to not shown explicitly)

The rablant "NT., JSI. Y



RADIANT INTENSITY:

$$J(s) = (2\pi k)^2 \tilde{W}^{(6)}(k_{S_1}, -k_{S_1}) \cos^2\theta$$

$$\tilde{N}^{(0)}(f_1,f_2) = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_1'f_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2'f_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2'f_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2' df_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2' df_2' df_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2' df_2' df_2' df_2' = \frac{1}{(2\pi)^4} \int W^{(0)}(f_1,f_2') e^{-r(f_2,f_2'+f_2,f_2')} df_2' d$$

ON THE SOURCE CONERENCE WO (5, 4) AND CONSEQUENTLY JUS) DEPEND BOTH ON THE AKI SOURCE INTENSITY

78-11

SCHELL - MODEL SOURCES *:

$$\mathcal{U}'(\underline{r},\underline{r}_{z},\omega) = g^{(o)}(\underline{r},-\underline{r}_{z},\omega) \quad (1)$$

$$\mathcal{N}^{(0)}(\underline{r}_{1},\underline{r}_{2},\omega) = \frac{W^{(0)}(\underline{r}_{1},\underline{r}_{2},\omega)}{\left(W^{(0)}(\underline{r}_{1},\underline{r}_{2},\omega)\right)} \left(W^{(0)}(\underline{r}_{2},\underline{r}_{2},\omega)\right)} \left[F_{\underline{r}_{2},\omega}\right]$$

$$\overline{T^{(0)}(\underline{r}_{1},\underline{r}_{2},\omega)} T^{(0)}(\underline{r}_{2},\underline{r}_{2},\omega)$$

$$N^{(0)}(\underline{r},\underline{r},\omega) = \prod^{(0)}(\underline{r},\omega) \prod^{(0)}(\underline{r},\omega) g^{(0)}(\underline{r},-\underline{r},\omega)$$
(2)

(DOCTORAL DISSERTATION, ANTENNA (a) THE MULTIPLE PLATE H.I.T, 1961), § 7.5 A.C. SCHELL :

(b) IEEE TRANS. AWTENANS AND PROPAGATION, AP-15, 187 (1967).

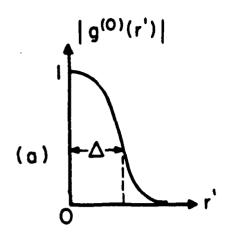
QUASI - HONOGENEOUS SOURCES*

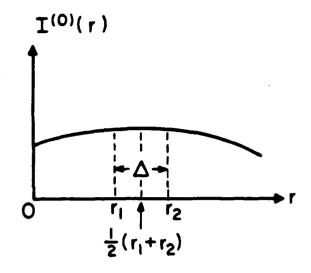
THESE ARE SCHELL-HODEL SOURCES FOR WHICH

(1) I (C,W) VARIES HUCH HORE SLOWLY WITH I q(0)(x,w) VARIES WITH I'= I-I.

- (2) LINEAR DIMENSIONS OF SOURCE >> CORECIATION DISTANCE IN SOURCE PLANE
- (3) LINEAR DIMENSIONS OF SOURCE 35 WAVELENGTH

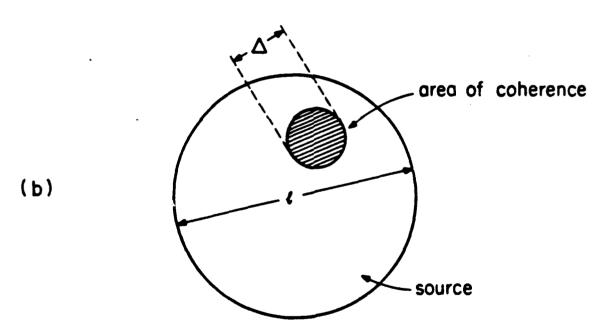
$$N^{(o}_{\underline{Y}_1,\underline{\eta}_1,\omega}) \simeq T^{(o)}(\frac{\underline{\eta}_1+\underline{\eta}_2}{2},\omega) \, g^{(o)}(\underline{\eta}_1-\underline{\eta}_2,\omega) \tag{3}$$





Degree of coherence (fast function)

Intensity (slow function)



Illustrating the concept of a quasi-homogeneous source.

- (a) The relative behavior of the degree of spatial coherence $\mu^{(0)}(\underline{r}_1,\underline{r}_2)$ $\equiv g^{(0)}(\underline{r}_1-\underline{r}_2)$ and of the intensity $I^{(0)}(\underline{r})$ of the light across the source.
- (b) The relative linear dimensions $\mathfrak{L}(>>\lambda)$ of the source and of the effective correlation length Δ of the light across the source. Such a source is always

globally incoherent: $\Delta \ll L$.

It is

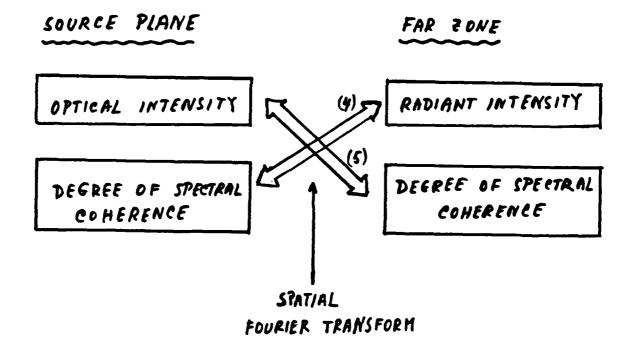
locally incoherent if $\Lambda \Rightarrow \lambda$ locally coherent if $\Delta >> \lambda$

RECIPROCITY RELATIONS FOR QUASI-HONDGENEOUS SOURCES

$$J(\underline{s}) = (2ih)^2 (\tilde{g}^{(i)}(h\underline{s}_{i}) \cos^2\theta \qquad (4)$$

$$\mu^{(6)}(r_{5}, r_{5}) = \frac{1}{c} \tilde{\mathbf{I}}^{(6)}[k(s_{u} - s_{e,l})] \qquad (5)$$

$$C = \tilde{I}^{(0)}(0) = \frac{1}{(2\pi)^2} \int I^{(0)}(1) d^2r \qquad (6)$$



NOTE: THE FIRST RECIPROPITY RELATION [Eq. (4)]

IMPLIES THAT THE ANGULAR DISTRIBUTION

OF THE RADIANT INTENSITY IS INDEPENDENT

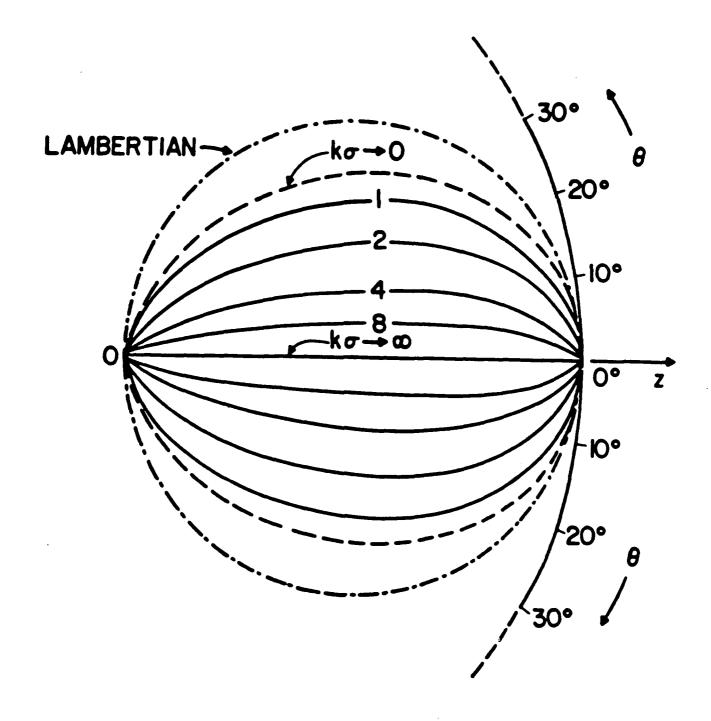
OF THE SHAPE OF THE SOURCE

$$g^{(0)}(r_1-r_2) = e^{-ir_1-r_2}i^{2}/26^{-2} \tag{7}$$

FIRST RECIPEOLITY RELATION [EQ. (4)] ONE FINDS THAT ON SUBSTITUTING FROM EG. (7) INTO THE

WHERE

$$J_{o} = \frac{(46)^{2}}{2\pi} \int I^{(o)}_{12} d^{2}$$
 (9)



Polar diagrams of the normalized radiant intensity $J(s)/J_o$ [Eq. (8)] from a Gaussian correlated quasi-homogeneous source, for different values of the r.m.s. width σ of the degree of spatial coherence [Eq. (7)]. The length of the vector pointing from the origin to a typical point on a curve labeled by a particular value of the parameter k σ represents the normalized radiant intensity in the direction of that vector. [After E. Wolf and W.H. Carter, Opt. Commun., 13, 205 (1975)].

LIMITING CASES

$$J(s) = J_{e} cos^{2} \theta e^{-\frac{1}{2}(46)^{2} cin^{2} \theta}$$
 [(8)]

As
$$\frac{h_6 \rightarrow 0}{(inconerent limit)}$$
 $\frac{7(5)}{5}$ $\rightarrow cos^2\theta$

(2)

As
$$h6 \rightarrow \infty$$
 (coherent limit) $\frac{3(3)}{J_o} \rightarrow 0$ when $\theta \neq 0$ $= 1$ when $\theta = 0$

 \mathfrak{E}

LANBERT'S LAN:

(2/)

FIRST RECIPROCITY RELATION [69.14)]:

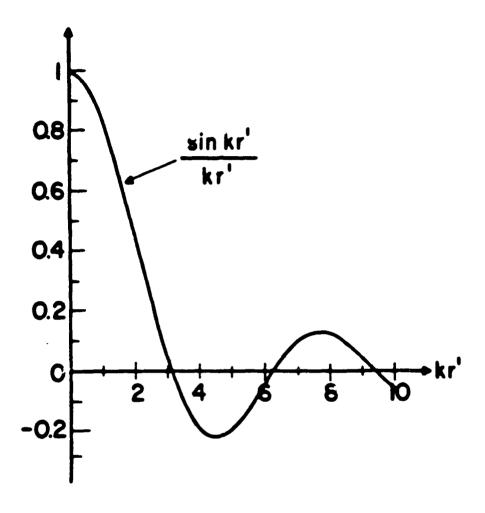
$$J(s) = (2\pi k)^2 (g^{(0)}(k_{S_2}) \cos^2 \theta$$

[(#)]

FROM EBS. (12) AND (4), TAKING FOURIER INVERSE, GIVES

$$g_{\text{cumb}}^{(0)}(\underline{r}_1 - \underline{r}_2) = \frac{S_{\text{ch}} R |\underline{y} - \underline{r}_2|}{R |\underline{r}_1 - \underline{r}_2|} + H.F.C. \quad (13)$$

(M.F.C. = HIGH SPATIAL-FREQUENCY CONTRIBUTION -DO NOT CONTRIBUTE TO FAR FIELD EYANESCENT WAVES).



The degree of spatial coherence of a quasi-homogeneous Lambertian source [Eq. (13) with high spatial-frequency contributions omitted].

ACROSS A QUASI-HOMOGENEOUS LAMRERTIAN SOURCE CORRELATION DISTANCE

FIRST ZERO OCCURS NHEN

ie. WHEN

$$|\vec{Y} - \vec{Y}| = \frac{\lambda}{2}$$

(*)

.. CORRELATION DISTANCE ACROSS LAMBERTIAM SOURCE IS

OF THE ORDER OF A WAYELENGTH,

A LAMBERTIAN SOURCE IS NOT STRICTLY SPATIALLY INCOMERENT. .e.

THESE RESULTS AGREE WITH KNOWN PROPERTIES OF RIACBODY PADATION.

$$J(\underline{s}) = (2\pi h)^2 \tilde{W}^{(0)}(h_{\underline{s_1}}, -h_{\underline{s_1}}) cos^2 \theta$$
 [(4), μ 33]
 $\underbrace{f_i \quad f_j}_{f_i} = \underbrace{f_j}_{f_j} = \underbrace{f_{ij}}_{f_{ij}} = \underbrace{f_{ij}}_{f_{ij$

ELEMENTS WILL GENERATE DENSITIES HAVE THE THE SAME DISTRIBUTIONS OF THE RADIANT INTENSITY. SAME LOW-FREQUENCY (f2 < A2) ANTI-DIAGONAL TW PLAMAR SOURCES WHOSE CROSS-SPECTRAL

•;

$$W'(x_1, x_2) = V'(x_1) + V'(x_2) + G^{(0)}(x_2 - x_2)$$
 [(12), p35]
Hore gonardly: $\mu^{(0)}(x_1, x_2)$

$$\widetilde{W}^{o}(B_{\underline{S}_{1},-}b_{\underline{S}_{1}}) = \frac{1}{(2\pi)^{3}} \iiint_{I^{o}(\underline{S}_{1})} \underbrace{I^{o}(\underline{S}_{1})}_{|MTemSITIES} \underbrace{I^{(o)}(\underline{S}_{1},\underline{T}_{2})}_{cone \, e \, e \, ne \, e} \underbrace{-i b_{\underline{S}_{1}, (\underline{S}_{1}-\underline{T}_{2})}_{J^{2}, (\underline{S}_{1},\underline{T}_{2})}_{J^{2}, (\underline{S}_{1},\underline{T}_{2})} \underbrace{-i b_{\underline{S}_{1}, (\underline{S}_{1}-\underline{T}_{2})}_{J^{2}, (\underline{S}_{1},\underline{T}_{2})}_{J^{2}, (\underline{S}_{1},\underline{T}_{2})}$$

4

^{*} E.COLLETT and E.NOLF, Oxf. L.H., 2,27 (1978); J. Oxf. Soc. Amer, 69, 942 (1979).

D. Me. GUIRE, Opt. Commun., 29, 17 (1974).

B.E. A. SALEH, Opt. Commun., 30, 135 (1979); B.E.A.SALEH and H.J. 185HID, Opt L.H. T. 302 (1882)

PARTIALLY COHERENT SOURCES WHICH GENERATE THE SAME DISTRIBUTION OF RADIANT INTENSITY AS A COMPLETELY COHERENT LASER SOURCE*

GAUSSIAN SCHELL-NODEL SOURCES:

$$q^{(0)}(\underline{x}) = e^{-v^2/26g^2}, \quad \underline{I}^{(0)} = Ae^{-v^2/26g^2}.$$
 (3)

1F

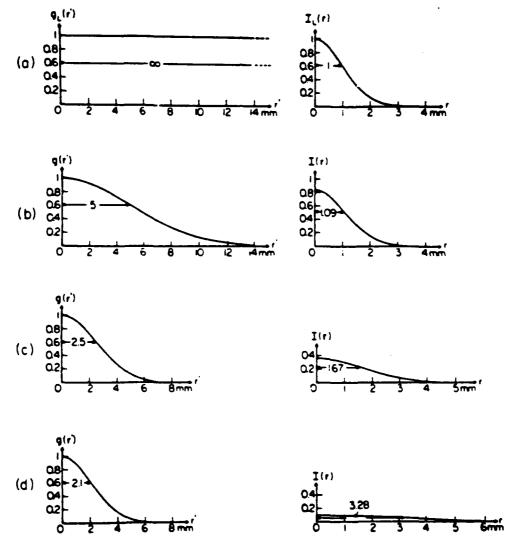
$$\frac{1}{6_1^2} + \frac{1}{(26_2)^2} = \frac{1}{(25_2)^2}, \quad A - \left(\frac{6_L}{6_2}\right) A_L \tag{3}$$

THE GAUSSIAN SCHELL- HODEL SOURCE WILL GENERATE SAKE DISTRIBUTION OF RADIANT INTENSITY AS LASER, WITH

$$g_L^{(0)}(\underline{x}') = 1$$
, $\underline{I}_L^{(0)}(\underline{x}) = A_L e^{-\tau^2/2 \xi^2}$ (4)

E. NOIF and E. COLLETT, Off. Commun, 25, 293 (1978)

Ø

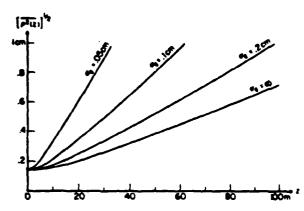


Illustrating the coherence and the intensity distributions across three partially coherent sources [(b), (c), (d)] which produce fields whose far-zone intensity distributions are the same as that generated by a coherent laser source [(a)]. The parameters characterizing the four sources are:

(a) $\sigma_g = -$, $\sigma_f = \delta_L = 1$ mm, A = 1 (arbitrary units) (b) $\sigma_g = 5$ mm, $\sigma_f = 1.09$ mm, A = 0.84 (c) $\sigma_g = 2.5$ mm, $\sigma_f = 1.67$ mm, A = 0.36 (d) $\sigma_g = 2.1$ mm, $\sigma_f = 3.28$ mm, A = 0.09.

The normalized radiant intensity generated by all these sources is $J(\theta)/J(0) = \cos^2\theta \exp\{-2(k\delta_{\perp})^2 \sin^2\theta\}$, $(\delta_{\perp} = 1 \text{ mm})$.

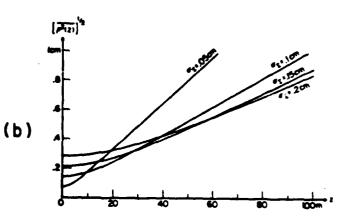
[After E. Wolf and E. Collett, Opt. Commun., 25, 293, 1978)].



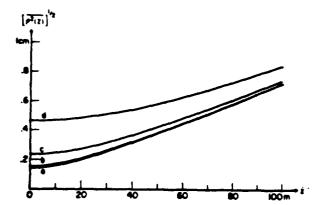
(o)

[^]c)

The r.m.s. beam radii for beams with the same initial r.m.s. beam radii ($\sigma_f = 0.1$ cm), but different degrees of coherence. The wavelength for each beam is 6328 A.

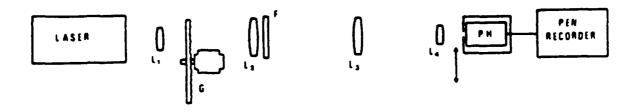


The r.m.s. beam radii for beams with the same degree of coherence $(a_g) \approx 0.2$ cm), but different initial r.m.s. radii. The wavelength for each beam is 6328 A.



The r.m.s. beam radii for beams with different initial r.m.s. beam radii and degrees of coherence, but with equal far field beam angles, θ_B . The parameters for the four beams are: (a) $\sigma_f = 0.1$ cm and $\sigma_g = \omega$, (b) $\sigma_f = 0.109$ cm and $\sigma_g = 0.5$ cm, (c) $\sigma_f = 0.167$ cm and $\sigma_g = 0.25$ cm and (d) $\sigma_f = 0.328$ cm and $\sigma_g = 0.21$ cm. The wavelength for each beam is 6328 A.

[After J. T. Foley and M.-S. Zubairy, Opt. Commun., 26, 297 (1978)].



A system used to test that sources with different coherence properties can generate identical angular distributions of the radiant intensity.

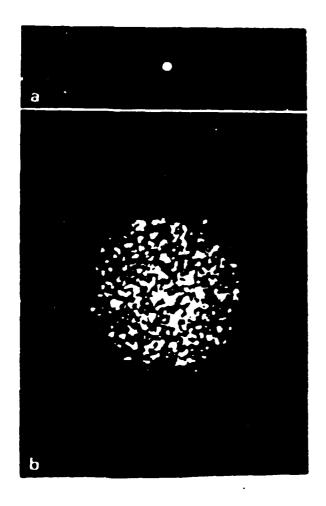
L₁, L₂, L₃, L₄: Lenses

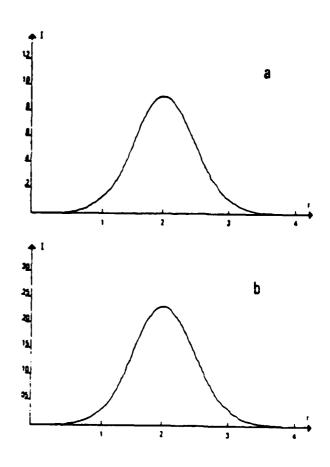
F: Amplitude filter

G: Rotating ground glass plate

PH: Photodetector

[After P. DeSantis, F. Gori, G. Guattari and C. Palma, Opt. Commun. $\underline{29}$, 256 (1979)]



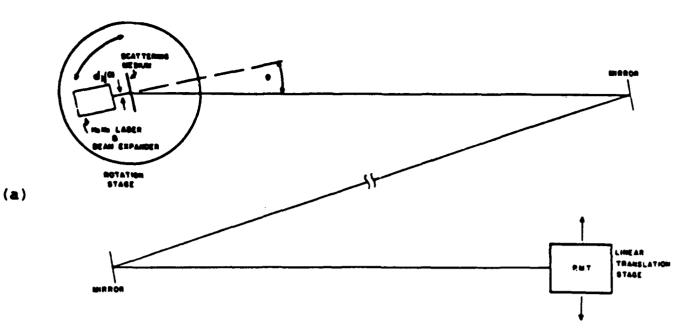


Intensity distribution across a coherent laser source (a), and across an "equivalent" partially coherent source (b).

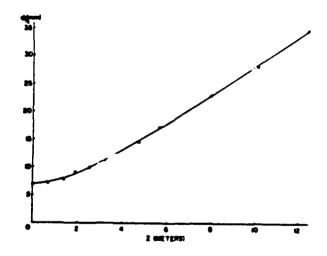
The measured angular distribution of intensity, I (in arbitrary but same units) in the far zone of fields generated by the two sources illustrated on the left.

(For experimental arrangement see p. 49)

Reproduced from P. DeSantis, F. Gori, G. Guattari and C. Palma, Opt. Commun., 29, 256 (1979).



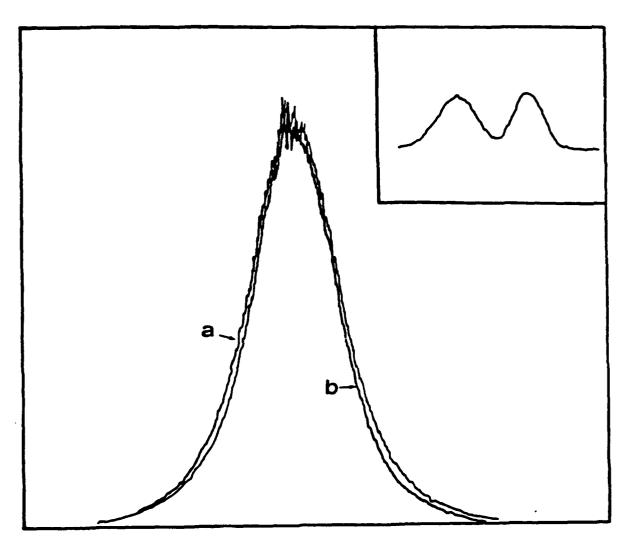
Schematic diagram of an experimental set up used to test some of the theoretical predictions relating to radiation from quasi-homogeneous sources.



(b)

Behavior of the effective beam diameter $d(z) = 2\sqrt{\rho^2(z)}$, as a function of distance from a quasi-homogeneous source. The solid line represents theoretical predictions; the points represent results of measurements, using the arrangement shown in (a) above.

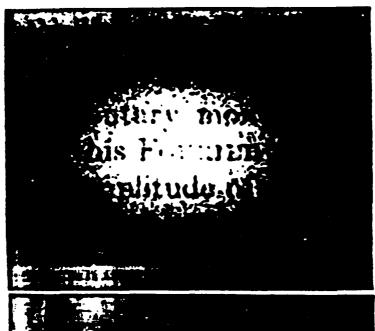
[After J. D. Farina, L. M. Narducci and E. Collett, Opt. Commun., 32, 203, (1980)].

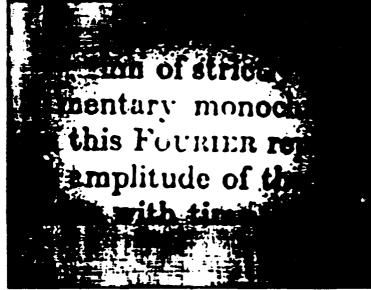


Far field intensity profile produced by the same phase screen illuminated by (a) the Gaussian ($\text{TEM}_{0,0}$) mode of a He-Ne gas laser, and (b) the donut ($\text{TEM}_{1,0}$) mode.

The inset shows the near field intensity profile of the illuminated phase screen under conditions (b). The vertical scale in the two runs has been adjusted to match the peaks of the intensity distribution. Thus, the two curves differ only by an overall scale factor.

After L.M. Narducci and J. Farina.





Illustrating the reduction of speckle effects by changing the degree of coherence of light forming the image.

The upper figure is a photograph of a text illuminated by spatially coherent He:Ne laser light. The speckles that are produced obscure the image, making the words nearly unreadable.

The lower figure was taken under the same conditions, except that the text was illuminated by light from a quasi-homogeneous (globally incoherent) source. It is seen that the speckles have been eliminated and as a result the text has become readable.

(After L. Narducci and J. Farina)

SOME METHODS FOR PRODUCING SOURCES OF CONTROLLED COHERENCE PROPERTIES

LIQUID CRYSTALS:

F. Scudieri, M. Bertolotti and R. Bartolino

Appl. Opt. 13, 181 (1974)

M. Bertolotti, F. Scudieri and S. Verginelli,

Appl. Opt. 15, 1842 (1976)

ROTATING ROUGH SURFACES:

P. de Santes, F. Gori, G. Guattari and C. Palma

Opt. Commun. 29, 256 (1979)

J.D. Farina, L.M. Narducci and E. Collett

Opt. Commun. 32, 203 (1980)

HOLOGRAPHIC FILTERS:

D. Courjon and J. Bulabois,

Proc. S.P.I.E. 194, 129 (1979)

ULTRASONIC WAVES:

Y. Ohtsuka and Y. Imai, J. Opt. Soc. Amer. 69, 684 (1979)

Y. Imai and Y. Ohtsuka, Appl. Opt. 19, 542 (1980)

Y. Ohtsuka, J. Opt. Soc. Amer. A 3, 1247 (1986)

IMAGING AND LENSLESS FEEDBACK SYSTEMS

J. Deschamps, D. Courjon and J. Bulabois,

J. Opt. Soc. Amer. 73, 256 (1983)

ACHROMATIC FOURIER TRANSFORM LENSES

G.M. Morris and D. Faklis

Opt. Commun. 62, 5 (1987)

ı

Source: Q(x,t), beatized in D

(4.2)

- 4TQ(E,t) V2V(x,t) - 1 32V(x,t)

* E. NOLF,

T. OPT. SOC. AMER., 72, 343 (1982);

I. OPT. SOC AMER. A, 3, 76 (1986).

Cross-comlation function of source distribution:

 $= \langle Q^*(g,t)Q(f,t^*) \rangle =$ (\$, 12, E)

 $\int \left| \int_{Q} (\underline{r}, \underline{r}_{2}, \tau) \right|^{2} d\tau < \infty$

Coss-specked density of sounce distribution:

 $= \frac{1}{2\pi} \int_{Q} (t_L t_\nu \tau) e^{i\omega \tau}$ $W_{\mathbf{Q}}(\underline{r},\underline{r},\omega)$

 $\int W_{q}(\underline{x},\underline{x},\omega)d^{3}r < \infty \qquad (5)$

From Eg. (5) and Schwanz' inequality

 $\iiint |W_{\alpha}(\underline{r_{1}},\underline{r_{2}},\omega)|^{2}d^{3}_{r_{1}}<\infty \qquad (6)$

$$\iiint\limits_{DD} |M_{q}(\underline{x}_{1},\underline{x}_{2},\omega)|^{2} d^{3}r, d^{3}x < \infty$$

[(9)]

$$W_{\alpha}(\underline{r}_{2},\underline{r}_{i},\omega)=W_{\alpha}^{*}(\underline{r},\underline{r}_{2},\omega)$$

$$\iint_{\partial D} W_0(\bar{x}_1, \bar{x}_2, \omega) f'(\bar{x}_1) f(\bar{x}_2) d^3 d^3 > 0$$
 (8)

Eq. (7)
$$\Longrightarrow$$
 Hermitean

Mercer's ophorem

$$N_{q}(\vec{x}, s_{t}, \omega) = \sum_{n} \lambda_{n}(\omega) \phi_{n}^{*}(\underline{x}, \omega) \phi_{n}(\underline{x}_{s}, \omega), \quad (9)$$

Star Star

$$\int W_{\mathbf{q}}(\underline{x}_{i},\underline{x}_{i},\omega) \, \phi_{i}(\underline{x}_{i},\omega) \, dx_{i} = \lambda_{i}(\omega) \, \phi_{i}(\underline{x}_{2},\omega), \quad (10)$$

$$\int \phi_{i}(\underline{x}_{i},\omega) \, \phi_{i}(\underline{x}_{i},\omega) dx_{i} = \sum_{i} x_{i}, \quad (11)$$

$$\lambda(\omega) > 0. \tag{12}$$

- (a) At least on eigenvalue
- (b) Expansion (9) holds whehe or met the set the 3 is complete
- (c) Expansion (9) is absolubly and uniformly convergent

Physical significance of expansion (9): Completly spakally whereat selected sources of Maked oscallabour

$$V_{Q}(\underline{\varsigma},\underline{\varsigma}_{2},\omega) = \sum_{\Lambda} \sum_{M} (\underline{\omega}) \phi_{M}^{*}(\underline{\varsigma},\underline{\omega}) \phi_{\Lambda}^{*}(\underline{\varsigma},\underline{\omega}) \qquad [(q)]$$

$$V_{Q}^{(n)}(\underline{\varsigma},\underline{\varsigma}_{2},\omega)$$

$$\mathcal{V}_{Q}^{(n)}(\underline{\tau}_{1},\underline{\tau}_{2},\omega) = \frac{\mathcal{V}_{Q}^{(n)}(\underline{\tau}_{1},\underline{\tau}_{2},\omega)}{\sqrt{\mathcal{V}_{Q}^{(n)}(\underline{\tau}_{1},\underline{\tau}_{2},\omega)}\sqrt{\mathcal{V}_{Q}^{(n)}(\underline{\tau}_{2},\underline{\tau}_{2},\omega)}}$$

$$\frac{1}{\sqrt{\lambda(\omega)|\phi'(\lambda'')|^2}\sqrt{\lambda''(\lambda'')|\phi''(\lambda''')|^2}}$$

$$= \frac{\phi_{m}^{*}(y, \omega)}{|\phi_{m}(y, \omega)|} \frac{\phi_{m}(y, \omega)}{|\phi_{m}(y, \omega)|}$$

$$\left| \int_{\mathbb{R}^{(n)}}^{(n)} (\underline{y}_1 \underline{y}_2, \omega) \right| = 1$$

:. EACH MODE IS SPATIALLY COMPLETELY COHERENT

(COHERENT-MODE REPRENTATION)

DENSITY OF THE SOURCE

167

Q, (W) ARE RANDOM COEFFICIENTS NITH

$$\langle a_{m}^{*}(\omega) a_{m}(\omega) \rangle = \lambda_{m} \langle \omega \rangle$$
 (4)

TURN

$$N_{q}(\underline{r},\underline{r},\omega) = \langle U_{q}^{*}(\underline{r},\omega) U_{(r_{2},\omega)} \rangle$$
 (19)

CROSS - SPECTRAL DENSITY OF THE FIELD DISTRIBUTION

$$(\Delta - \frac{1}{2} \frac{\partial^2}{\partial t}) V(\underline{r}, t) = -4\pi Q(\underline{r}, t)$$

$$W_{Q}(\underline{x}_{1},\underline{x}_{2},\omega) = \frac{1}{2\pi} \int \langle Q^{*}(\underline{x}_{1},+)Q(\underline{x}_{2},++z) \rangle e^{i\omega t}$$

$$W_{V}(x_{1},x_{2},\omega) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \langle V(x_{1},t)V(x_{2},t+\tau) \rangle e^{i\omega t} = (21)$$

$$(\nabla_{i}^{2} + k^{2})(\nabla_{i}^{2} + k^{2})W_{i}(x_{i}, x_{j}, \omega) = (4\pi)^{2}W_{i}(x_{i}, x_{j}, \omega)$$
 (22)

COHERENT - MODE REPRESENTATION OF RADIATED FIELD

SOURCE: Wa (I, I, U) =
$$\sum \lambda_{\mu} \phi_{\mu}^{*}(S, \omega) \phi_{\mu}(I_{2}, \omega)$$

$$= \langle U_{\alpha}^{*}(\underline{r}, \omega) U_{\alpha}(\underline{r}, \omega) \rangle \qquad [(m)]$$

[[3]

USING EQ. (22):

FIELD:
$$V_{\mu}(\bar{x}, \bar{x}_{\varepsilon, \omega}) = \sum_{n} \lambda_{n} \psi_{n}^{*}(\bar{x}_{\varepsilon, \omega}) \psi_{n}(\bar{x}_{\varepsilon, \omega})$$

$$= \langle U_{\mu}^{*}(\bar{x}_{\varepsilon, \omega}) U_{\nu}(\bar{x}_{\varepsilon, \omega}) \rangle_{\omega} \qquad (24)$$

$$U_{p}(g\omega) = \sum_{m} a_{m} f_{m}(\underline{r}, \omega) \qquad (25)$$

$$V_{p}(g\omega) = \int_{0}^{\infty} d_{m}(\underline{r}, \omega) \frac{e^{i\hat{R}[\underline{r}-\underline{r}']}}{|\underline{r}-\underline{r}'|} d^{\frac{2}{p'}} \qquad (26)$$

 $\{V(x,t)\}$

$$\frac{\text{Source}}{\text{Source}}: W_{\mathbf{R}}(\underline{r},\underline{r}_{2},\omega) = \sum_{i} \lambda_{i}(\omega) \phi_{i}^{*}(\underline{r},\omega) \phi_{i}^{*}(\underline{r}_{2},\omega) \quad [(9)]$$

$$= \langle U_{\alpha}^{*}(x, \omega) U_{\alpha}(x_{2}, \omega) \rangle_{\omega}$$
 [(19)]

F/E1D:

$$\phi_{n}(\underline{r}, \omega) - \psi_{n}(\underline{r}, \omega) = \int \phi_{n}(\underline{r}, \omega) \frac{e^{ik_{1}r_{-1}r_{1}}}{|\underline{r}_{-1}|} d^{3}r^{i}$$
 [[26]]

FIELD:

 $W_{(x_n, x_n, \omega)} = \sum_{i} \sum_{(\omega)} \varphi_i^*(\underline{x}_{i, \omega}) \varphi_i(\underline{x}_{i, \omega})$

$$= \langle \bigcup_{\mathbf{v}}^{\mathbf{x}}(\mathbf{f}, \omega) \bigcup_{\mathbf{v}} (\mathbf{f}_{\mathbf{s}}, \omega) \rangle$$

(92)

COMPARE WITH

 $W_{\mathbf{a}}(\mathbf{x}, \mathbf{z}, \omega) = \sum_{i} \lambda_{i}(\omega) \phi_{i}^{*}(\underline{\mathbf{r}}, \omega) \phi_{i}(\underline{\mathbf{r}}, \omega)$

[(6)]

$$= \langle U_{\alpha}^{*}(\varsigma,\omega) U_{\alpha}(\varsigma_{2},\omega) \rangle$$

[(60)]

SOURCE:

Uq (I,w) = Z a (w) of (I,w)

[(8)]

(82)
$$(\alpha, 2, 2, \omega) = \sum_{i=1}^{n} \lambda_{i}^{*}(\omega) \lambda_{i}^{*}(x, \omega) \psi_{i}(x, \omega) = \sum_{i=1}^{n} \lambda_{i}^{*}(\omega, 2, \omega) \psi_{$$

ELEMENTARY COHERENT SOURCE OSCILLATIONS OFILLS. COMERENT FIELDS. EACH HODE IS A COMPLETELY SPATIALY THIS EXPANSION IS A MODE REPRENTATION OF PARTIFILY COMERENT WAYE, OF FREQUENCY W, GENERATED BY

APPLICATIONS

Coherence properties of laser modes

Statistical properties of speckles

Light propagation through the atmosphere

Scattering from fluctuating media

CROSS - SPECTRAL DENSITY

CYELES

Q HIRROR Š

(STR.) O (INITIAL DISTR.)

W(E, gr, w)

41814 4

M. C. (2, w)

A TRTATATE

W2 (9, 5, 0)

* E. WOLF and G.S. AGARWAL, J. Opt. Soc. Amer., A, 1,541(1984)

$$M_j(g_j,g_k,\omega) = \langle U_j^*(g_k,\omega) U_j(g_k,\omega) \rangle$$

$$U_{j+1}(g,\omega) = \int L(g,g',\omega) U_{j}(g',\omega) d' g', \qquad (j = 0,1,2,...), \qquad (2)$$

$$W_{j+1}(g,g,\omega) = \iiint_{A,A} (g,g,\omega) L(g,g,\omega) W_{j}(g',g',\omega) d_{g}^{2} / d_{g}^{2} , \qquad (3)$$

FOR STEADY STATE:

$$M_{+}, (p, p, \omega) = \sigma(\omega) W, (p, p, \omega)$$

SINCE W(3,5,W) 70,

ઉ

 $\iiint W(g', g', \omega) L^*(p, p', \omega) L(p_2, p', \omega) d'p', d'p' = \sigma(\omega) W(p_2, p_2, \omega)$ (6)

(BASIC INTEGRAL EQUATION OF PRESENT THEORY)

NATURE OF SOLUTIONS OF INTEGRAL EQUATION (6).

$$\int L(\mathbf{r}_{1},\mathbf{r}_{2},\mathbf{u}) \phi_{m}(\mathbf{r}_{2},\mathbf{u}) d\mathbf{r}_{2}^{2} = \phi_{m} \phi_{m}(\mathbf{r}_{1},\mathbf{u})$$

$$A$$
(7)

$$\int_{A} L^{*}(f_{2}, f_{1}, \omega) \chi_{m}(f_{2}, \omega) df_{2}^{2} = \beta_{m} \chi_{m}(f_{1}, \omega)$$
(8)

$$\beta_m = \alpha_m^* \tag{9}$$

$$\int_{\infty}^{\infty} \langle P, \omega \rangle \chi_{m}(p, \omega) dp^{2} = \int_{\infty}^{\infty} (10)$$

BI-ORTHOGONAL EXPANSION OF LIBER, W):

$$L(\hat{y}, \hat{y}_{2}, \omega) = \sum_{m} \alpha_{m}(\omega) \phi_{m}(\hat{y}, \omega) \chi^{*}(\hat{y}_{2}, \omega) \qquad (11)$$

* P.M. MORSE AND H. FESHBACH, <u>METHODS OF</u>

MATHEMATICAL PHYSICS (MS3), Vol T, \$1,919-920.

EQUATION (6) CAN BE SHOWN TO BE NECESSARILY OF THE FORM IF THERE IS NO DEGENERACY, SOLUTIONS OF THE INTEGRAL

$$W_{\kappa}(\underline{g},\underline{g},\omega) = \lambda_{\kappa}(\omega) \phi_{\kappa}^{*}(\underline{g},\omega) \phi_{\kappa}(\underline{g},\omega), \quad (22)$$

WITH EIGENVALUES

$$\mathcal{O}_{K}(\omega) = \alpha_{K}^{*}(\omega)\alpha_{K}(\omega), \qquad (13)$$

WHERE

$$\int \mathcal{L}(\mathcal{B}, \mathcal{R}, \omega) d_{\mathcal{R}} = \mathcal{A}_{\mathcal{R}}(\omega) d_{\mathcal{R}} = \mathcal{A}_{\mathcal{R}}(\omega) d_{\mathcal{R}}(\mathcal{P}, \omega) \int_{\mathcal{R}} \mathcal{P}(\mathcal{P}, \omega) d_{\mathcal{R}}(\mathcal{P}, \omega) d_{\mathcal{R}}(\mathcal{P}, \omega) d_{\mathcal{R}}(\mathcal{P}, \omega) d_{\mathcal{R}}(\mathcal{P}, \omega) d_{\mathcal{R}}(\mathcal{P}, \omega)$$

EQUATION (7) IS THE FOX-LI EQUATION FOR (HONDCHRUHATIC) LASER MODES [A.G. FOX and T. LI, Bell Syd. Tech. I, 40, 453 (1961)].

$$W_{\kappa}(P_{i},\underline{r}_{i},\omega) = \lambda_{\kappa}(\omega) \phi_{\kappa}^{*}(P_{i},\omega) \phi_{\kappa}(\underline{r}_{i},\omega) \phi_{\kappa}(\underline{r}_{i},\omega).$$
 [(12)]

DEGREE OF SPECTRAL COHERENCE AT FREQUENCY W OF FACE MODE:

CONPLETE SPATIAL COHERENCE AT FREQUENCY W.

SPECTRAL DENSITY:

* M. BERTOLOTTI et al. Nuovo Cimento, 38, 1505 (1965-).

$$W_{(g,g,\omega)} = \lambda_{\kappa}(\omega) \phi^*(g,\omega) \phi_{(g,\omega)}$$

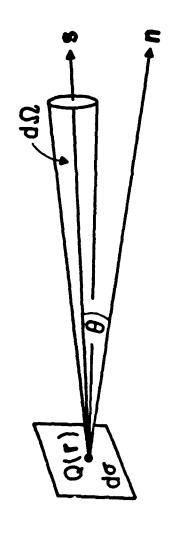
$$(21) \quad d^{2}(\mathbb{R}, \mathbb{R}, \mathbb{R}, \mathbb{R}) = (2, \mathbb{R}, \mathbb{R}, \mathbb{R}) + (2, \mathbb{R}, \mathbb{R}) = (2, \mathbb{R}, \mathbb{R})$$

FOX-U HODES

$$\mu_{\kappa}(g_{1},g_{2},\omega) = \frac{W_{\kappa}(g_{1},g_{2},\omega)}{[W_{\kappa}(g_{1},g_{2},\omega)]^{2}} \frac{W_{\kappa}(g_{1},g_{2},\omega)}{[W_{\kappa}(g_{1},g_{2},\omega)]^{2}} = \frac{1}{2} |W_{\kappa}(g_{1},g_{2},\omega)|^{2} = 0$$
(18)

7 = | 2 18 18 18 1 = 1 [[" (s,g,o)]" [["(p,g,o)]" TK (B. Ez, T) JK (g, g, r) =

FOUNDATIONS OF RADIOMETRY



$$d\mathcal{E}_{\nu} = B_{\nu}(\mathbf{r}, \mathbf{s}) \cos \theta \ d\sigma \ d\Omega \ dt$$

Radiated power:
$$P_{\nu} = \int d\sigma \int d\Omega \ B_{\nu}(\mathbf{r}, \mathbf{s}) \cos \theta$$
 (2)

$$= \int_{\sigma} E_{\nu}(\mathbf{r}) d\sigma = \int_{\sigma} J_{\nu}(\mathbf{s}) d\Omega$$

(3)

$$E_{\nu}(r) = \int B_{\nu}(r,s) \cos \theta \, d\Omega = \text{Radiant emittance}$$
 (4)

$$J_{\nu}(\mathbf{s}) = \cos \theta \int_{\sigma} |\mathbf{r}, \mathbf{s}| d\sigma = \text{Radiant intensity}$$
 (5)

EQUATION OF PADIATIVE ENERGY TRANSFER

SPACE DENSITY OF RADIATION

$$u_{\gamma}(\underline{x}) = \frac{1}{c} \int_{\mathbb{R}} B_{\gamma}(\underline{x},\underline{s}) d\underline{\omega} \Omega_{4} \qquad (septral)$$

3

$$F_{\gamma}(\underline{r}) = \int_{\mathcal{B}_{\gamma}} B_{\gamma}(\underline{r},\underline{s}) \underline{s} d\Omega \qquad (vector)$$

(&)

(MARGINAL RELATIONS)

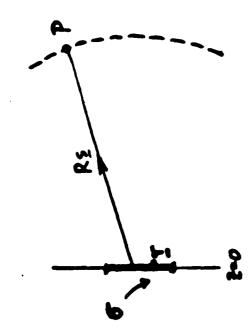
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RADIATIVE TRANSFER IN FREE SPACE

$$S. \nabla B_{y}(r,s) = -\alpha_{y}(r,s) B_{y}(r,s) + \int \beta_{y}(r,s,s') B_{y}(r,s') d\Omega_{x}' + D_{y}(r,s)$$
(6)

(10a)

$$B_{y}(\underline{c},\underline{s}) = B_{y}(\underline{c}',\underline{s})$$
 (10)



$$F_{y} = \int W(R_{2}, R_{2}, \nu) R^{2} d \Omega$$

$$(2\pi) \quad \text{Optical "intervity}$$

$$(4R \rightarrow \infty)$$

$$F_{\sigma} = \int_{\partial \Omega} d\Omega \int_{\partial \Sigma} B_{\sigma}(x, \underline{s}) \cos \theta \quad (22)$$

$$\vec{B}_{y}(z;s) = \left(\frac{A_{x}}{2\pi}\right)^{2} c_{xy}\theta \int W(z+fz',z-fz',v)e^{-iA_{x}\cdot z'}d^{2}z' \qquad (13)$$

J. OPT. SOC. AMER., 64, 1219 (1974). E. W. MARCHAND AND E. NOLF, OPT. COMMON, 6, 305 (1972); A. WALTHER, J. OPT. SOC. AHER., 58, 1256 (1968).

20

$$\vec{B}_{y}^{(i)}(\underline{r},\underline{s}) = \left(\frac{4}{2\pi}\right) \cos \theta \int M(\mathbf{r} + f\underline{r}', \underline{r} - f\underline{r}', \nu) e^{-ik\underline{s}\cdot\underline{r}'} e^{ik} \qquad [(i.s)]$$
(3-0)

$$B_{Y}^{(2)}(\underline{r}, \underline{s}) = \left(\frac{4}{2\pi}\right)^{2} \cos \int W(\underline{r}, \underline{r}, Y) e^{-ih\underline{s}\cdot(\underline{r}-\underline{r}')} d^{2} / (14)$$
(14)

$$\mathcal{B}_{r}^{(\alpha)}(\underline{r},\underline{s}) \neq \mathcal{B}_{r}^{(r)}(\underline{r},\underline{s}) \qquad (1.5)$$

$$\mathcal{B}^{\mu f} \qquad \mathcal{F}^{(e)} = \mathcal{F}^{(i)} \qquad (16)$$

V. I. TATARSKII (1971); G.I. OVCHINNIKOV AND V.I. TATARSKII (1972) E. H. MARCHAND AND E. NOLE, J. OPT. SOC. AMER., 64, 1273 (1974) A. WALTHER, J. OPT. SOC. AMER., 63,1622 (1973); 64, 1275 (1974) 1.5 DOLIN (1964)

RECENT RESEARCH ON FOUNDATION OF RADIOMETRY*

1.) Restriction to globally incoherent sources

(Quasi-homogeneous sources)

2.) Short wavelength limit $(\lambda \rightarrow 0)$

(Asymptotic limit: $k = 2\pi/\lambda \rightarrow \infty$)

^{*} J. FOLEY and E.WOLF, Opt. Commun. <u>55</u>, 236 (1985).

K. KIM and E. WOLF, J. Opt. Soc. Amer. A 4, 1233 (1987).

G.S. AGARWAL, J.T. FOLEY and E. WOLF, *Opt. Commun.* <u>62</u>, 67 (1987).

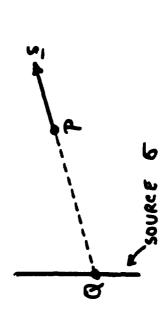
Review of earlier researches: E. WOLF, *J. Opt. Soc. Amer.* <u>68</u>, 6 (1978); A.T. FRIBERG, *Opt. Eng.* <u>21</u>, 927 (1982).

FOR A WINSI - HUMOGENEEUS SJUKEE

$$N^{(0)}(\underline{x}_1, \underline{x}_2, \nu) = \underline{L}^{(0)}(\underline{x}_1 + \underline{x}_2, \nu) g^{(0)}(\underline{x}_1 - \underline{x}_2, \nu)$$
 [6, (3), transp. 36]
$$|NTEMSITY COHERENCE (FAST)$$

ASYMPTOTIC LIMIT AS & --

GEONETRICAL INTERPRETATION:



B, (P, E) ~ R'S, I'(0, Y) q''(B.E, Y)

[(1/4)]

CONE FORMED BY RAYS

JOINING P TO ALL

SOURCE POINTS

(0 B,(P, E) ≥ 0

(2) $B_{y}(P_{y}E) = 0$

- IF QEG (S WITHIN CONE)
- 1F Q&O (3
- Q¢ € (\$ OUTSIDE CONE)
- CONSTANT ALONG EVERY S-DIRECTION (3) By (9, 2)
- TAROUGH P ; I.e. CATISPIES EQUATION
- OF RADIATIVE TRANSFER IN FREE SPACE

Special CASE i LIMBERTIAN SUNLE

[(17a)]

$$q^{(s_1-s_2,r)} = \frac{\sin(\hbar |s_1-s_2|)}{\hbar |s_1-s_2|}$$
 [Eq. (13), transp. 42]

$$\tilde{g}^{(c)}(k_{2_{1}},v) = \frac{1}{2\pi R^{2}s_{2}}$$
 (s,=0.18)

8)

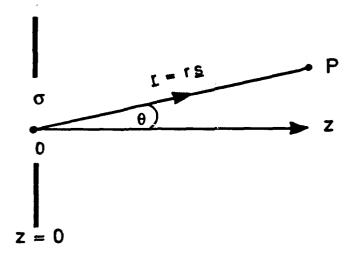
$$\begin{bmatrix} \mathbf{g}_{\mathbf{y}}(\mathbf{p}, \underline{\mathbf{z}}) \end{bmatrix}_{\text{lansertion}} \sim \frac{1}{2\pi} \mathbf{T}^{(0)}(\mathbf{p}, \mathbf{r}) \quad \text{if Qeo} \quad \text{(19)}$$

$$\sim 0 \quad \text{if Qeo} \quad \text{(19)}$$

NOTE: THE RADIANCE NOW DEPENDS
ONLY ON THE SOURCE INTENSITY



EFFECTS OF SOURCE CORRELATIONS ON THE SPECTRUM OF EMITTED LIGHT



Planar secondary quasi-homogeneous source σ

Same source spectrum, $S^{(o)}(\omega)$, at every source point

Reciprocity formula (4) on transparency 38 implies that spectrum in the far zone is

$$S^{(\infty)}(\underline{\tau},\omega) = \frac{J_{\omega}(\underline{s})}{\tau^2} = \frac{\underline{k}^2 A}{\tau^2} S^{(\omega)} \widetilde{\mu}^{(o)}(\underline{k}\underline{s},\omega) \cos^2 \theta \qquad (1)$$

A = area of source

 $\widetilde{\mu}^{(0)}{}_{=}$ Fourier transform of degree of spectral coherence of light in source plane $[g\to\mu]$

The spectrum of the far field depends not only on the source spectrum $S^{(0)}(\omega)$ but also on the coherence properties of the source.

In general, the normalized spectrum of light changes on propagation.

RADIATION FROM A PRIMARY SOURCE

$$(\nabla_{1}^{2}+\underline{\lambda}^{2})(\nabla_{2}^{2}+\underline{\lambda}^{2})W_{V}(\underline{x},\underline{x},\omega)=(4\pi)^{2}W_{Q}(\underline{x},\underline{x},\omega)$$
 [(7)]

RADIATION FROM A PLANAR, HOMOGENEOUS SECONDARY SOURCE

$$(\nabla_i^2 + \underline{k}^2)(\nabla_2^2 + \underline{k}^2) W_{V}(\underline{Y}_i, \underline{Y}_i, \omega) = 0 \qquad (2 \ge 0) \qquad (7a)$$

B.C.:
$$W_{V}(\underline{\tau}, \underline{\tau}, \omega) \Big|_{z=0} = W_{V}(\underline{\tau}, \underline{\tau}, \omega) \quad \underline{\tau}, \underline{\tau}' \in \mathcal{E}$$
 (14)

THE DEGREE OF SPECTRAL COHERENCE (A = V or Q)

$$\mu_{A}(\underline{\tau}_{1},\underline{\tau}_{2},\omega) = \frac{W_{A}(\underline{\tau}_{1},\underline{\tau}_{2},\omega)}{\sqrt{W_{A}(\underline{\tau}_{1},\underline{\tau}_{2},\omega)}}, (0 \leq |\mu_{A}| \leq 1)$$
 (15)

NORMALIZED SPECTRUM

$$S_{A}(\underline{\tau},\omega) = \frac{S_{A}(\underline{\tau},\omega)}{\int S_{A}(\underline{\tau},\omega)d\omega} \left(\int S_{A}(\underline{\tau},\omega)d\omega - 1\right)$$
(16)

SCALING LAW [E Wolf, Phys. Rev. Lett. 56 1370 (1986)]

A SUFFICIENCY CONDITION FOR THE NORMALIZED SPECTRUM OF LIGHT PRODUCED BY A PLANAR, HOMOGENEOUS SECONDARY SOURCE TO BE THE SAME THROUGHOUT THE FAR ZONE AND ACROSS THE SOURCE ITSELF IS THAT THE DEGREE OF SPECTRAL COHERENCE OF THE LIGHT DISTRIBUTION ACROSS THE SOURCE HAS THE FORM

$$\mu_{i}^{(n)}(\Sigma_{i}^{i}-\Sigma_{i}^{i},\omega) = f[k(\Sigma_{i}^{i}-\Sigma_{i}^{i})], \quad (k \cdot \xi = \xi^{E}) \quad (77)$$

I.E. THAT IT IS A FUNCTION OF THE VARIABLE

$$\xi = \lambda(\underline{\tau}_2' - \underline{\tau}_1') = 2\pi \frac{\underline{\tau}_2' - \underline{\tau}_1'}{\lambda}$$
 (18)

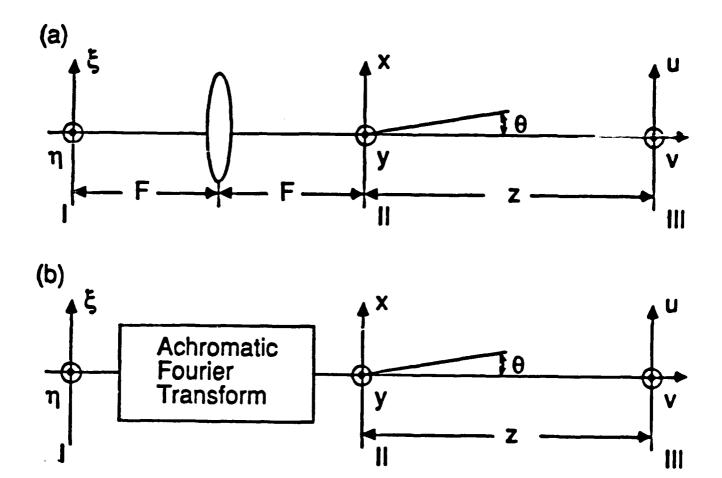
ONLY.

$$\mu_{\nu}^{(0)}(\underline{r}_{2}'-\underline{r}',\omega) = f[k(\underline{r}_{2}'-\underline{r}')], (k=\frac{\omega}{c}=\frac{2\overline{n}}{\lambda})$$
 [(17)]

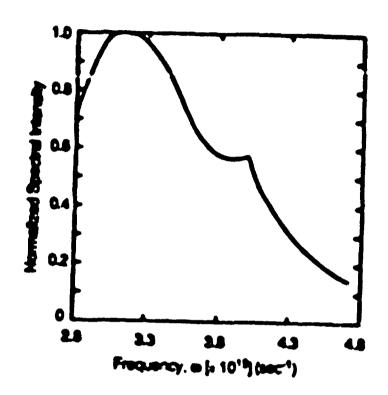
EXAMPLES :

BLACKBODY SOURCES LAMBERTIAN SOURCES

$$\mu_{V}^{(\bullet)}(I_{2}'-I_{2}',\omega) = \frac{\sin(k|I_{2}'-I_{2}'|)}{k|I_{2}'-I_{2}'|}$$
(19)

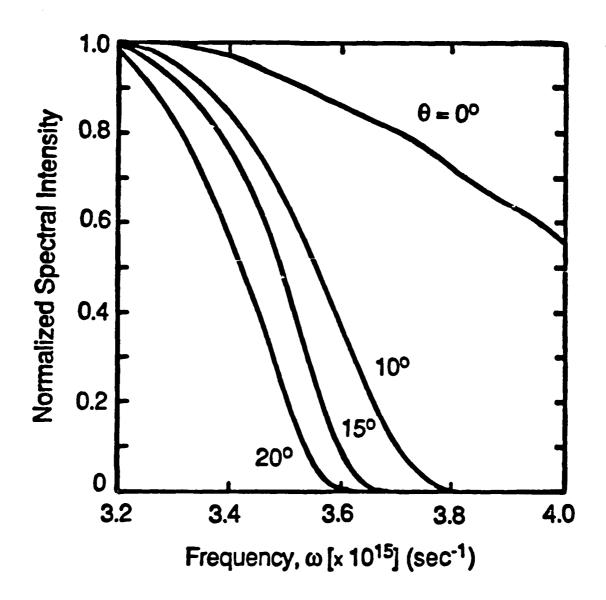


AFTER G. M. MORRIS AND D. FAKLIS, OPTICS COMMUNICATIONS 62, 5 (1987).



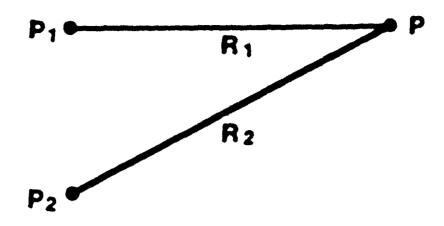
(9) SCALING LAW SATISFIED
AFTER G. M. MORRIS A. D. FAIGLS.

OPTICS COMMUNICATIONS 62.5 (1967).



(b) SCALING LAW NOT SATISFIED

AFTER G. M. MORRIS AND D. FAKLIS, OPTICS COMMUNICATIONS 62, 5 (1987).



SOURCE ENSEMBLES: $\{Q(P_1,\omega)\}, \{Q(P_2,\omega)\}$

FIELD ENSEMBLE: (U(P. w))

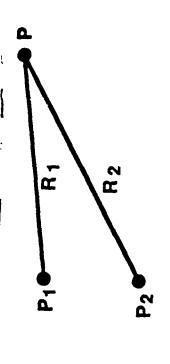
$$U(P, \omega) = Q(P_1, \omega) \frac{e^{ikR_1}}{R_1} + Q(P_2, \omega) \frac{e^{ikR_2}}{R_2}$$

$$k = \frac{\omega}{C}$$
(9)

SPECTRUM OF THE FIELD AT P:

$$S_{V}(P, \omega) = \langle U^{*}(P, \omega)U(P, \omega) \rangle$$
(10)

*E. Wolf, Phys. Rev. Lett. 58, 2646(1987).



$$S_{V}(P, \omega) = \langle Q^{*}(P_{1}, \omega)Q(P_{1}, \omega) \rangle \frac{1}{R_{1}^{2}} + \langle Q^{*}(P_{2}, \omega)Q(P_{2}, \omega) \rangle \frac{1}{R_{2}^{2}} + \left[\langle Q^{*}(P_{1}, \omega)Q(P_{2}, \omega) \rangle \frac{e^{ik(R_{2} - R_{1})}}{R_{1}R_{2}} + c_{ij} \right]$$

$$S_{Q}(\omega)$$

$$S_{Q}(\omega)$$

$$S_{Q}(\omega)$$

$$S_{V}(P, \omega) = S_{Q}(\omega) \left[\frac{1}{R_{1}^{2}} + \frac{1}{R_{2}^{2}} \right] + \left[W_{Q}(P_{1}, P_{2}, \omega) \frac{e^{ik(R_{2} - R_{1})}}{R_{1}R_{2}} + cc. \right]$$
 (11)

 \therefore Sv(P, ω) IS **NOT** PROPORTIONAL TO S $_{\Omega}(\omega)$, IN GENERAL

EXEPTIONAL CASES:

(1) $W_{Q}(P_1, P_2, \omega) \equiv 0$: Uncorrelated

(INCOHERENCE)

(2) $W_{Q}(P_1, P_2, \omega) \propto S_{Q}(\omega)$, $R_2 = R_1$: Completely correlated

(COHERENCE)

WITH THE CHOICE $R_2 = R_1 = R$, Eq.(11) REDUCES TO

$$S_{V}(\omega) = 2 S_{Q}(\omega) [1 + \text{Re } \mu_{Q}(\omega)]$$
 (12)

$$S_V(\omega) = \frac{2}{R^2} S_V(P, \omega) = REDUCED FIELD SPECTRUM$$
 (12a)

 $\mu_{O}(\omega) = Degree of correlation between the sources$

$$\mu_{Q}(\omega) = \frac{W_{Q}(P_{1}, P_{2}, \omega)}{S_{Q}(\omega)}$$

$$= \frac{\langle Q^{\bullet}(P_{1}, \omega)Q(P_{2}, \omega) \rangle}{S_{Q}(\omega)}$$
(13)

$$0 \leq \left| \begin{array}{c} \mu_Q(\omega) \right| \leq 1 \\ \text{UNCORRELATED} \end{array}$$

SOURCE:

$$S_Q(\omega) = A e^{-(\omega - \omega_0)^2/2\delta_0^2}$$
 $(\delta_0/\omega_0 <<1)$

$$\mu_{Q}(\omega) = a e^{-(\omega - \omega_{1})^{2}/2\delta_{1}^{2}} - 1$$
 $(\delta_{1}/\omega_{1} << 1, a \le 2)$

FIELD:

$$S_{V}(\omega) = A^{1}e^{-(\omega - \omega_{0}^{1})^{2}/2\delta_{0}^{12}}$$

$$A' = \frac{2Aa}{R^2} e^{-(\omega - \omega_0')^2/2(\delta_0^2 + \delta_1^2)}$$

$$\omega_0' = \frac{\delta_1^2 \omega_0 + \delta_0^2 \omega_1}{\delta_0^2 + \delta_1^2}$$

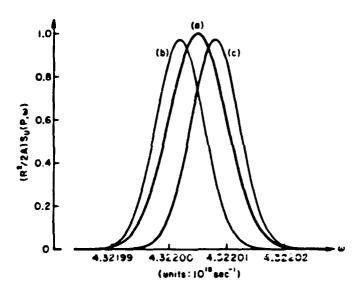
$$\frac{1}{\delta_0^{12}} = \frac{1}{\delta_0^2} + \frac{1}{\delta_1^2}$$

$$\omega_0^{\prime} < \omega_0 \implies \omega_1 < \omega_0$$

$$\omega_1 < \omega_0$$

$$\omega_0^{\bullet} > \omega_0^{\bullet} \Rightarrow \omega_1^{\bullet} > \omega_0^{\bullet}$$

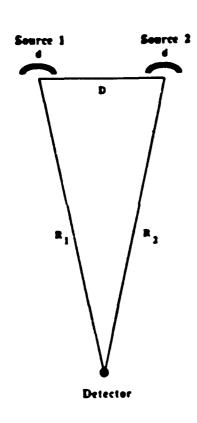
$$\omega_1 > \omega_0$$

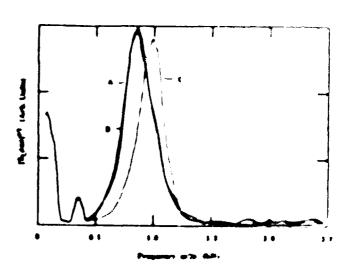


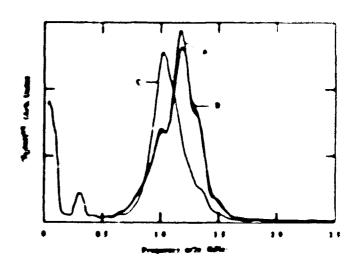
From E. Wolf, *Phys. Rev. Lett.* **58**, 2646 (1987)

EXPERIMENTAL TEST WITH ACOUSTICAL SOURCES

M.F. Bocko, D.H. Douglass and R.S. Knox *Phys. Rev. Lett.* **58**, 2649 (1987)

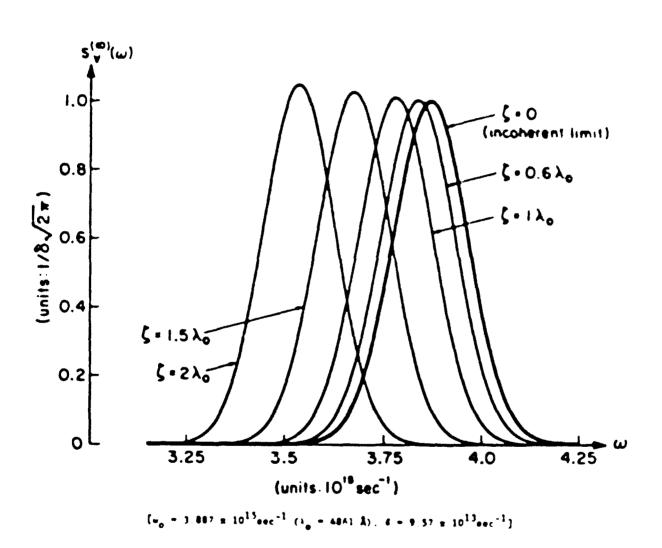






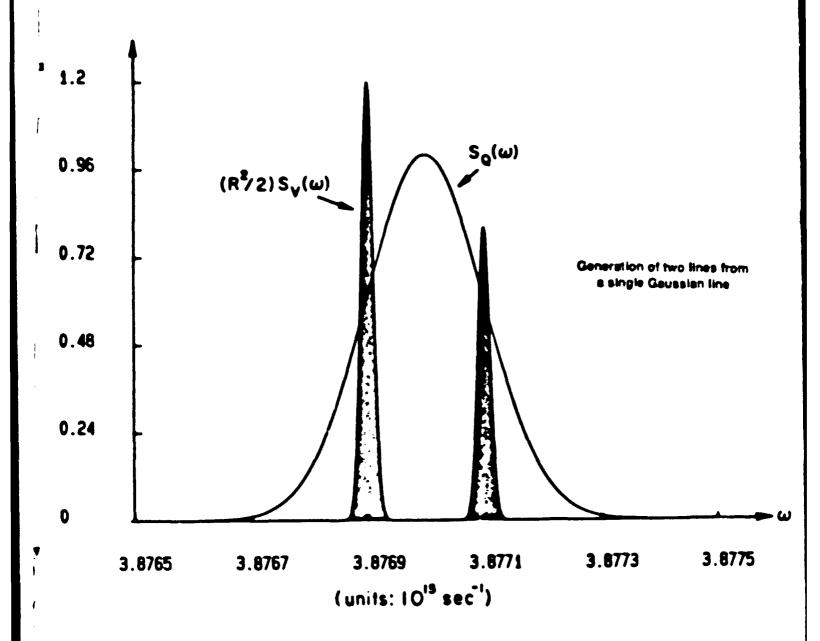
REDSHIFTS WITH THREE-DIMENSIONAL SOURCES

Similar results hold for spectra of fields radiated by three-dimensional sources*

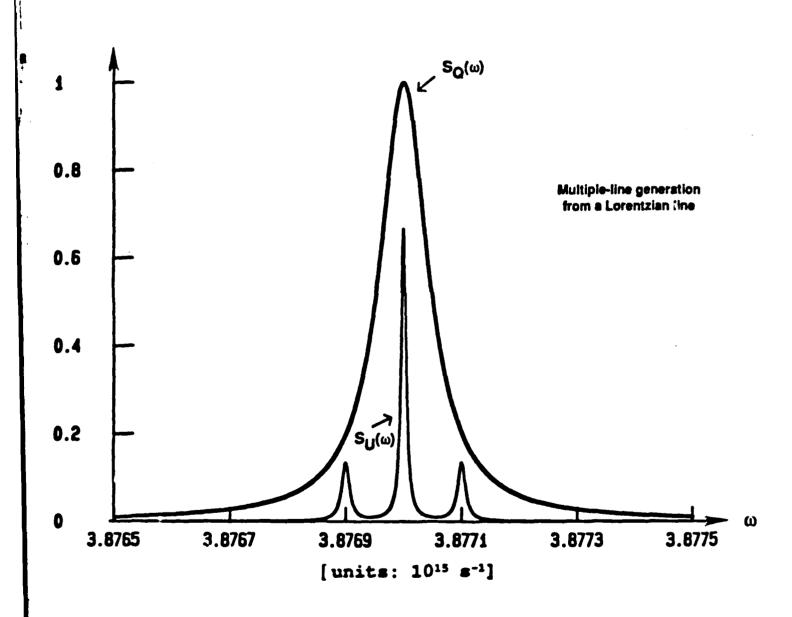


* E. Wolf, Nature 326, 363 (1987); Opt. Commun. 62, 12 (1987).

OTHER KINDS OF SPECTRAL MODULATION BY CONTROL OF SOURCE CORRELATIONS



After A. Gamliel and E. Wolf, Opt. Commun., in press



After A. Gamliel and E. Wolf, Opt. Commun., in press.

REFERENCES

PUBLICATIONS DEALING WITH CHANGES DUE TO SOURCE CORRELATIONS IN THE SPECTRUM OF EMITTED RADIATION

(a) Theoretical

- E. Wolf, "Invariance of spectrum of light on propagation", Phys. Rev. Lett. 56, 1370-1372 (1986).
- E. Wolf, "Non-cosmological redshifts of spectral lines", Nature 326, 363-365 (1987).
- E. Wolf, "Redshifts and blueshifts of spectral lines caused by source correlations", Opt. Commun. 62, 12-16 (1987).
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- A. Gamliel and E. Wolf, "Spectral modulation by control of source correlations", Opt. Commun. 65, 91-96 (1988).
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(b) Experimental

- G. M. Morris and D. Faklis, "Effects of source correlation on the spectrum of light", Opt. Commun. 62, 5-11 (1987).
- M. F. Bocko, D. H. Douglass and R. S. Knox, "Observation of frequency shifts of spectral lines due to source correlations", Phys. Rev. Lett. 58, 2649-2651 (1987).

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F Gori, G Guattari, C Palma and G Padovani, 'Observation of optical redshifts and blueshifts produced by source correlations', Opt Commun, in press

W. Knox and R. S. Knox, "Direct observation of the optical Wolf shift using white-light interferometry", Opt. Lett. (submitted), see also abstract of postdeadline paper PD21, Annual Meeting of the Optical Society of America (Rochester, NY), October, 1987. J. Opt. Soc. Amer. A. §, No. 13, P151 (1987).

CECOM CENTER FOR NIGHT VISION AND ELECTRO-OPTICS ARMY APPLICATIONS OF COHERENCE PHENOMENA

SOME APPLICATIONS - COHERENCE

- 1. LASER PROTECTION
- 2. LASER DETECTION
- 3. MOTION/VIBRATION SENSING
- 4. COHERENT IMAGING -ACTIVE/PASSIVE
- 5. COMMUNICATIONS

Related Programs

Coherence Filters - Physical Optics Corp. U. S. Army Natick R & D Center

Acoustic - Optic coherence deflection filters - MTL

In-house Research in coherent filters - WPAFB

Photorefractive material research - CNVEO



Modern Coherence Theory

Attendees List

18 May 1988

Center for Night Vision & Electro-Optics:

Rudy Buser
Robert Rohde
Mark Norton
Ed Sharp
Mark Savan
Richard Utano
Wayne Hovis
Mary Miller
L.N. Durvasula
Andy Kennedy
Tom Colandene
Suresh Chandra

Al Pinto
Gary Wood
Bill Clark
Gerri Daunt
Martin Lenhart
Gertrude Kernfield
Fred Carlson
Andy Mott
Charles Martin
Jim Habersat
Greg Salamo
C. Ward Trussell

University of Rochester:

Professor Wolf Brian Cairns Nicholas George Tom Stone

Other:

William Carter, NRL, #767-2453 Suzanne St. Cyr, Polaroid